

Advantages of steel section over reinforced section or concrete member :-

* Higher strength \Rightarrow
 \Rightarrow It becomes higher ($\frac{\text{strength}}{\text{weight}}$) ratio compared to concrete structure.

$$\text{Higher } \left(\frac{S}{W}\right)_{s.s} \geq \left(\frac{S}{W}\right)_{c.c}$$

\Rightarrow More economical (due to higher ($\frac{\text{strength}}{\text{weight}}$) ratio)
 \Rightarrow Ductility of material measured by percentage of elongation

When percentage of Elongation $> 15\% \Rightarrow$ Ductile
 (ex - steel, Al)

When ^{5% of} percentage of Elongation $\leq 15\% \Rightarrow$ Intermedi
 (ex - Mg)

When percentage of Elongation $< 5\% \Rightarrow$ Brittle mate
 (ex - cast iron, Cu)

\Rightarrow Easily repairable and maintainable.

\Rightarrow High durability.

\Rightarrow 100% scrap value.

\Rightarrow Overall cost of structure is less.

Disadvantages

- corrosion problem (due to corrosion thickness decreases)
- Less time resistance (So it reduces f_y and f_u values)

Type of Steel

- (1) Standard steel
- (2) Fusion welding steel
- (3) High tensile steel.

(1) Standard steel

→ Used for static loads. Ex. - Fe 410 S

→ Carbon = 0.23 - 0.25%

→ (P.E) Percentage Elongation upto/after fracture = 23%

→ Welding if $t \leq 20$ mm (t = thickness of steel member)

(2) Fusion welding steel

→ It is used for dynamic and impact loads [Ex. - Fe 410 WA, Fe 410 WB]

→ Carbon = 0.20 - 0.25%

→ Percentage Elongation upto/after fracture = 23%

→ Welding if $t > 20$ mm (t = thickness of steel member)

(3) High tensile steel

→ It is used for high tensile force. Ex. → Fe 550, Fe 570

→ Carbon = 0.27%

→ Percentage elongation up to/ after fracture = 20%

Properties of structural steel

(1) Physical properties:-

specific gravity = $s = 7.85$

young's modulus = $E = 2 \times 10^5$

co-efficient of thermal expansion = $\alpha = 12 \times 10^{-6} / ^\circ C$

Poisson's ratio = $\mu = 0.25$ (IS: 800 - 1984)

$\mu = 0.30$ (IS: 800 - 2007)

$\Rightarrow E = 2C(1 + \mu) \Rightarrow C = \text{shear modulus}$

$\Rightarrow E = 3K(1 - 2\mu) \Rightarrow K = \text{bulk modulus}$

(2) Mechanical properties

Steel	fy value			fu
	t < 20mm	t = 20-40mm	> 40mm	
Standard and fusion welding steel	250	240	230	410
High tensile steel	350			570

2nd half

Standard rolled steel section

(i) Rolled steel tube section (or) hollow section

(ii) Rolled steel bars [square bars and round bars]

(a) IS 800 = Indian standard square section (designated by side)

(b) IS 800 = Indian standard round section (designated by dia.)

(iii) Rolled steel flats (when $t \geq 5$ mm) ex: IS 800 F 10

(iv) Rolled steel plates (when $t \geq 5$ mm) ex: IS PL (100 x 12)

(v) Rolled steel sheets (when $t < 5$ mm) &

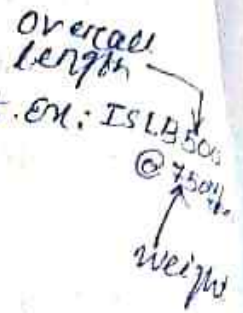
(vi) Rolled steel strips (IS ST)

Ex: ISSQ 100 \Rightarrow side of square = 100 mm
 ISRO 120 \Rightarrow dia = 120 mm

(vi) I-section

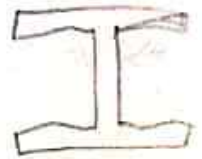
(vii) Rolled steel I-section

\Rightarrow Designated by overall depth and weight. Ex: ISLB 500 @ 75 kg/m



Types of rolled I-section

- (1) ISJB (Indian Standard Junior Beam)
- (2) ISLB (Indian Standard Light Beam)
- (3) ISMB (Indian Standard Medium weight Beam)
- (4) ISWB (Indian Standard Wide flanged Beam)
- (5) ISHB (Indian Standard Heavy Beam)



(viii) Rolled steel (C) channel section

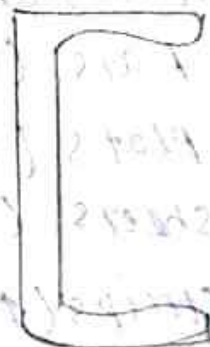
\rightarrow Designated by overall depth and weight.

Ex - ISMC 500 @ 750 $\frac{N}{mm}$

\downarrow \downarrow
 Overall length weight

Types of rolled steel (C) channel-section.

- (a) ISJC = Indian standard junior channel section.
- (b) ISLC = Indian standard light channel section.
- (c) ISMC = Indian standard medium weight with sloping flange.
- (d) ISMLP = Indian standard medium weight with parallel flange.
- (e) ISQC = Indian standard gate channel section.



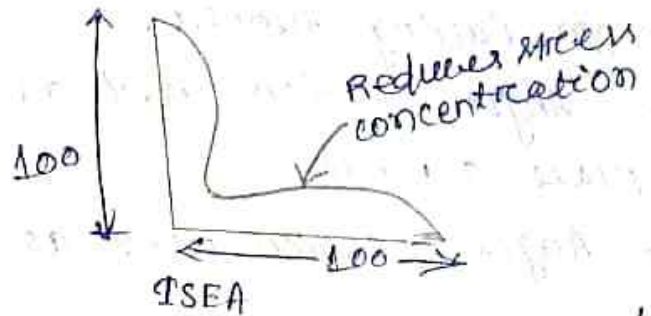
(iv) Rolled steel angle section

→ It is designated by its leg width and thickness

ISL - ISA (100 x 100 x 10)

leg width

thickness



(Indian Standard Equal Angle)

(i) ISEA → Indian standard equal angle

(ii) ISUA → Indian standard unequal angle

(iii) ISBA → Indian standard Bulb Angle

NOTE

Angle section: most suitable when

(i) for compression member ⇒ Equal angle section
(So used as a struts) ($\because I_{zz} = I_{yy}$ (or) $C_{zz} = C_{yy}$)
and r_{min} is more as compared to unequal angle section)

(ii) for tension member ⇒ Unequal angle section with longer leg is connected to gusset plate.

($I_{zz} > I_{yy}$ (or) $C_{zz} > C_{yy}$)

(iii) ISBA has more stiffness, more rigidity but it has more weight, that's why not used in structure. But particularly used in ship building construction

→ Flat section is best section for tension member

use of angle section

→ In case of principal rafter in roof truss in

→ In lacing member.

→ Angle section used as stiffener member in plate girder.

→ Angle section used as cleat member in foundation.

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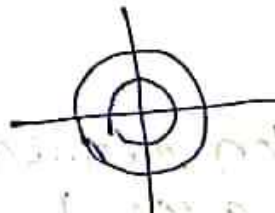
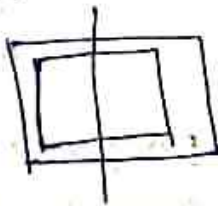
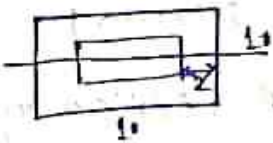
(X) Roofed steel tube / Hollow section :-

→ Hollow sections are designated by their outside dimension and thickness.

→ Hollow sections are best section for tension, compression & torsion.

→ Box type section is desirable for when torsion is dominant.

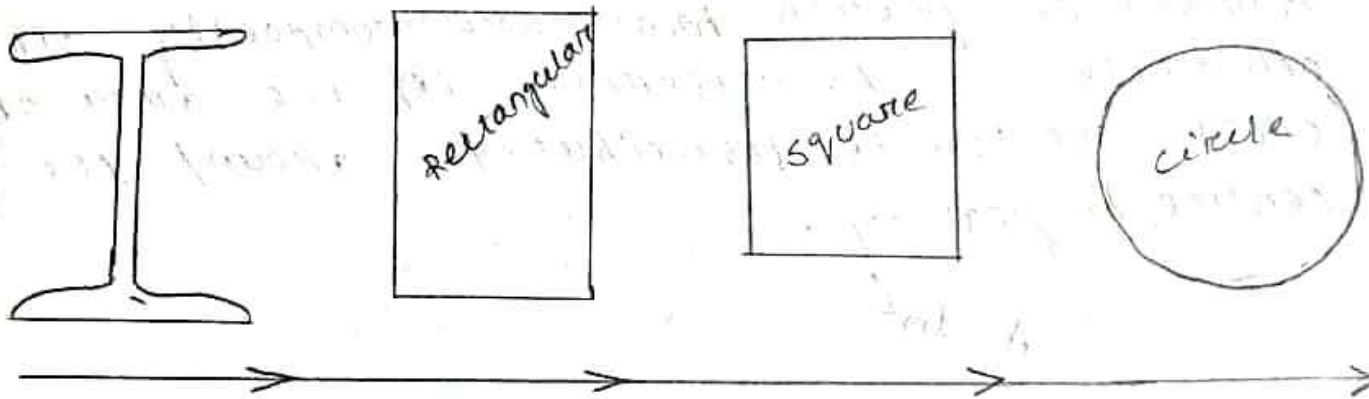
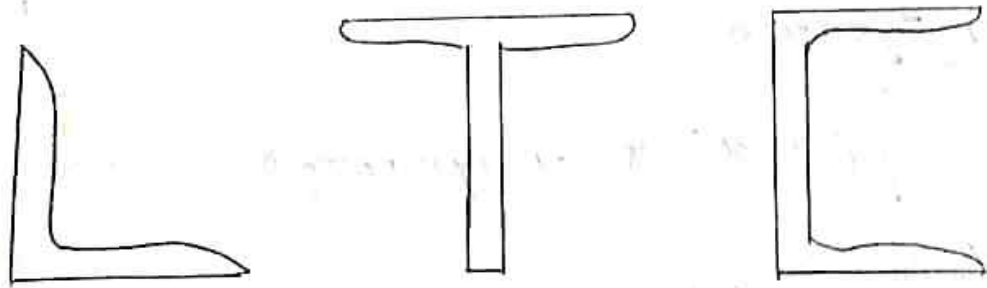
→ Ideal steel member is to with stand axial compressive force i.e., circular hollow section.



For same cross sectional area or weight a circular hollow section gives higher moment of inertia (MI) and polar moment of inertia and radius of gyration about any diameter axis as compared to solid circular section. Hence circular hollow section is more efficient and economical to resist axial compression.

strongest section as a compression member
is equal solid circular section.

most suitable section as a compression member
equal to hollow circular section.



(compressive)
strength
&

(torsional)
strength)

As a beam

in increasing order as a strongest section

→ ~~most strongest & suitable section~~ is 'I'

→ ~~most strongest~~ 'I' section as a beam is ~~ISWB~~

→ most suitable 'I' section as a beam is ~~ISMB~~

As a compression member
 → Strongest 'I' section as a compression member
 is ISMB.
 → Most suitable 'I' section as a compression member is ISHB

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λ ↑
Euler
 F
 cr

Radius of gyration

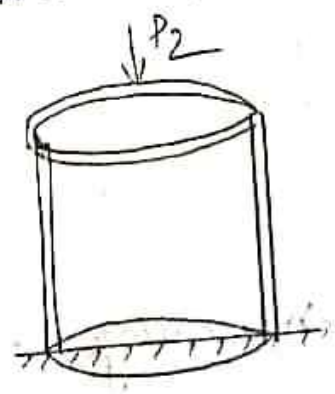
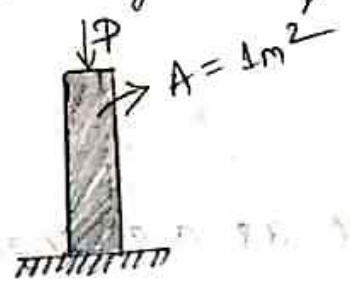
$$r = \sqrt{\frac{I}{A}}$$

(Radius of gyration)

$$r_{min} = \sqrt{\frac{I_{min}}{A}}$$

(Minimum radius of gyration)

Radius of gyration means how compactly or otherwise the material in the area of cross section is distributed around the centre of gravity.



$P_2 > P_1$

so, $r_{min} \uparrow \Rightarrow$ material scattered $\uparrow \Rightarrow$ buckling \downarrow
 always more radius of gyration is aim for engineer
Slenderness ratio :- for any structural member

→ It is used for long column.
 → It is denoted by λ

$$\lambda = \frac{l}{r_{min}}$$

where,

l = effective length

r_{min} = minimum radius of gyration.

$\lambda \uparrow \Rightarrow \pi_{min} \downarrow \Rightarrow$ stability decreases \Rightarrow No Buckling of column

Euler's critical compressive load carrying capacity

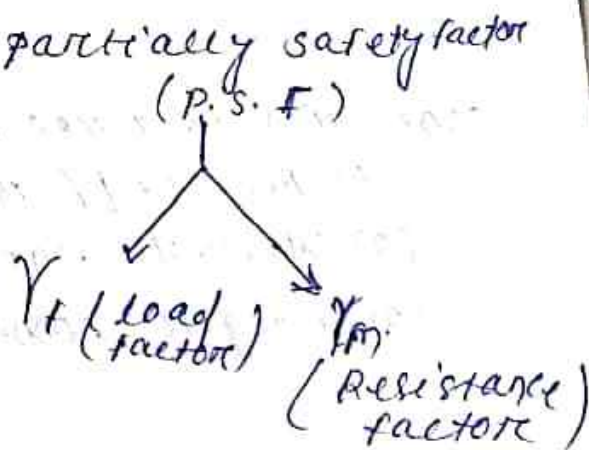
$$\begin{aligned}
 P_{crit} &= \frac{\pi^2 EI}{l^2} \\
 \downarrow \\
 \text{cripping load} &= \frac{\pi^2 EI}{(KL)^2} \quad [\because l = Kl] \\
 &\quad \uparrow \text{depend on end condition} \\
 &= \frac{\pi^2 EA \pi^2}{l^2} \quad \left[\because I = A \pi^2 \right. \\
 &\quad \left. \pi = \sqrt{\frac{I}{A}} \right] \\
 &= \frac{\pi^2 EA}{\left(\frac{l}{\pi}\right)^2} \\
 &= \frac{\pi^2 EA}{\lambda^2} \quad [\because \frac{l}{\pi} = \lambda]
 \end{aligned}$$

Load and Load combinations :-

limit state design (L.S.D) \Rightarrow partially safety factor (P.S.F) (IS: 800-2007)

Load factor (γ_f)

$$\gamma_f = \frac{\text{Design load}}{\text{characteristics load}}$$



\Rightarrow Design load = $\gamma_f \times$ characteristics load

Resistance factor (γ_m)

$$\gamma_m = \frac{\text{characteristics strength}}{\text{Design load strength}}$$

① Load factor (γ_f) value
 ② Load combination

DL + LL	→	1.5	
DL + WL	→	1.5	
DL + (WL/EL) + LL	→	1.2	(for ROOF trusses)

(2) Resistance factor (γ_m) value

→ Resistance factor against yield stress (f_y)
 $\Rightarrow f_y \Rightarrow \gamma_{m0} = 1.1$ (Also against buckling)
 → Resistance factor against ultimate stress (f_u)
 $f_u \Rightarrow \gamma_{m1} = 1.25$

→ Resistance factor for connection (γ_{m1}) is γ_{mf} (or)
 $\gamma_{mb} = 1.25$ [Expect weld connection]
 → Resistance factor for weld connection
 $\rightarrow \gamma_{mw} = 1.25$ [shop fabrication]
 $\rightarrow \gamma_{mw} = 1.5$ [field fabrication]

- connection is three types
- (1) Riveted / Bolted connection
 - (2) Welded connection
 - (3) Hanger connection

$$\gamma_m = \frac{\text{Characteristic strength}}{\text{Design strength}}$$

Limit state design

limit state of collapse	limit state of serviceability
(1) limit state of strength ⇒ (1) yielding (2) buckling (3) flexure (4) shear	→ Deformation → Deflection → Vibration → Corrosion → Fibre → Fatigue checks
(2) stability ⇒ (1) Against sliding (2) Against overturning	

NOTE

The requirement to be satisfied for safety of structural member and structural connection in design action should be less than equals to design strength.

$$\boxed{\text{Design action} \leq \text{Design strength}}$$

Design action is due to design value of internal forces (shear force, bending moment, twisting moment and torsion) occurs due to external load ^{design due to material strength}

$$\text{Factored (or) Design load} = \gamma_f \times \left(\begin{array}{l} \text{permissible safe} \\ \text{characteristics} \\ \text{working} \end{array} \right) \text{ load}$$

$$\text{Design strength} = \frac{\text{characteristic strength}}{\gamma_m}$$

Ch-02. STRUCTURAL STEEL FASTENERS AND CONNECTIONS

BOLTED CONNECTION:-

Types of Bolt

(1) Black or unfinished or bearing type or slip type

- these are used for light structure subjected to static load.
- It allow slip of plate and load transfer through the bearing action.
- It is made up of low carbon steel i.e, mild steel

Ex:- M5 to M36

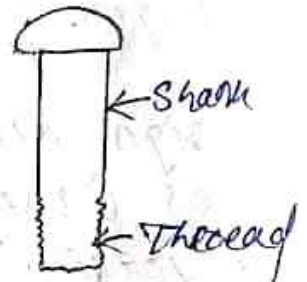
But most common M6, M8, M10, M12, M16, M20, M24, M30

(Number indicates shank diameter of bolt)

$$\text{Shank area of bolt} = A_s$$

$$\text{Thread/net area of bolt} = A_n$$

$$= 0.78 A_s$$



Grade of bolt varies from 4.6 to 8.8

4.6 grade of bolt means $f_{ub} = 400 \text{ MPa (or) } \text{N/mm}^2$

$f_{yb} = 400 \times 0.6 = 240 \text{ MPa}$

where, f_{yb} = yield stress of bolt

f_{ub} = ultimate stress of bolt

Ques Grade of bolt = 5.6 -

Grade of

$$f_{ub} = 5 \times 100 = 500 \text{ MPa}$$

$$f_{yb} = 500 \times 0.6 = 300 \text{ MPa}$$

Ques Grade of bolt = 7.2

$$f_{ub} = 7 \times 100 = 700 \text{ MPa}$$

$$f_{yb} = 700 \times 0.2 = 140 \text{ MPa}$$

Ques

M20

$$\text{Shank Area } (A_s) = \frac{\pi}{4} \times 20^2$$

$$= 314 \text{ mm}^2$$

(Thread area) $A_{tb} = 0.78 \times A_s$

$$= 0.78 \times 314$$

$$= 245 \text{ mm}^2$$

(2) HSTFG (High Strength Friction Grip Bolt)

→ These bolts are fixed by developing maximum tension in bolt such that plates develop maximum compression between them.

→ These bolt does not allow slip of bolt so load transfer takes place due to the friction between the plates.

→ These are used in structures which subjected to dynamic loads, vibration, impact loads & fatigue loads & most suitable for structures subjected to reversal of stresses.

EN - 10.9 S

- 12.9 S

NOTE

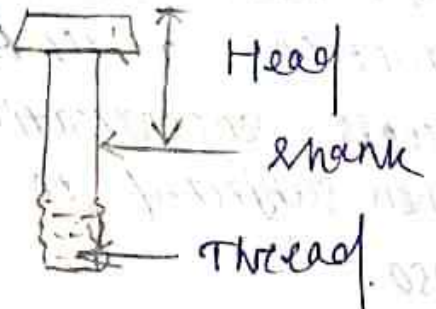
Bolt is designated by M d L

M d L

where, M = metric size

d = shank dia.

L = shank length



$$T_{db2} = \frac{0.9 A_n f_{ub}}{\gamma_{m1}}$$

$$= \frac{0.9 \times 148 \times 400}{1.25} = 129024 \text{ N}$$

$$= 129 \text{ kN}$$

$$\Rightarrow T_{db2} = 129 \text{ kN}$$

So, smaller value is taken

$$T_{db1} = 68.51 \text{ kN}$$

$$V_{dcb} = 45.08 \text{ kN}$$

$$V_{dcpb} = 130.56 \text{ kN}$$

\therefore Design strength of bolt = V_{db} = smaller of $V_{dcb}, V_{dcpb}, T_{db}$

$$\Rightarrow V_{db} = V_{dcb} = 45.08 \text{ kN}$$

no. of bolts required to resist factor load 562.5 kN

$$\Rightarrow n = \frac{P_d}{V_{db}}$$

$$= \frac{562.5}{45.08}$$

$$= 12.47 \text{ nos}$$

NOTE

cover plate thickness $\approx 13 \text{ nos}$

for single cover butt joint thickness of cover plate = $1.25 t_{min}$

for double cover butt joint thickness of cover plate = $\frac{5}{8} t_{min}$

Types of bolted joint (or) connection:-

There are 3 types of connection:-

- ✓ Shear type connection \Rightarrow (1) Lap (2) Butt
- X (2) Hanger type \Rightarrow Tension type connection
- X (3) Combined shear and ^{tension} bending type \Rightarrow Bracket connection

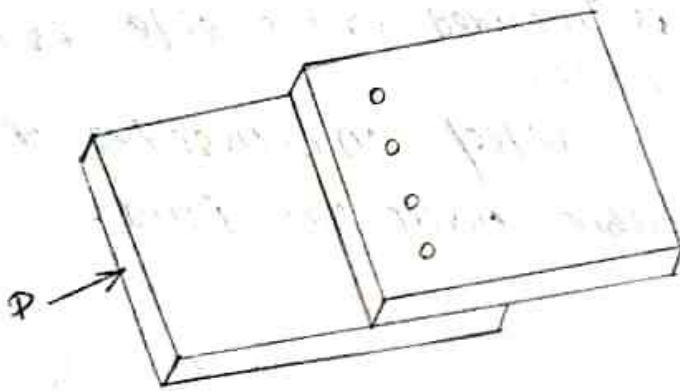
(1) Shear type connection

It is of two types

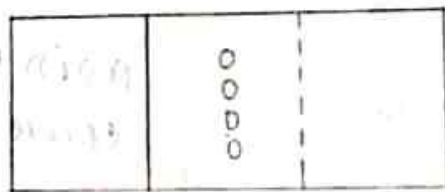
- (1) Lap connection
- (2) Butt connection

(1) Lap joint

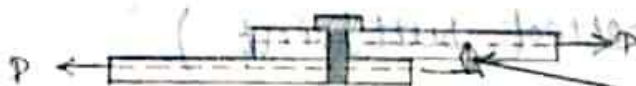
\Rightarrow The two members to be connected are overlapped & connected together. Such a joint is called as lap joint.



(Lap joint)



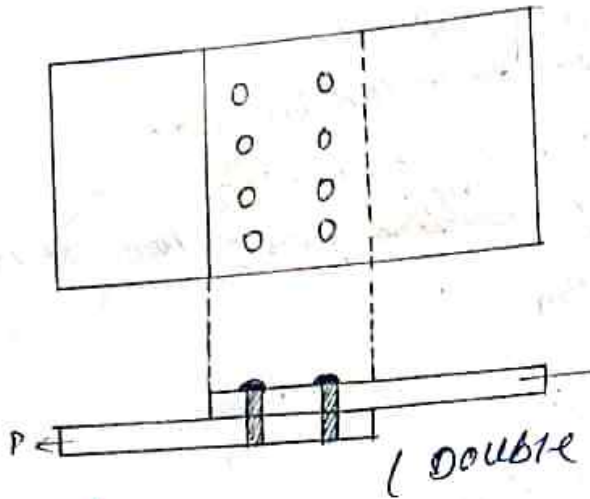
Plan



(Elevation)

$e =$ eccentricity = cause moment ~~but~~; so tension failure may occur

(Single bolted lap joints)

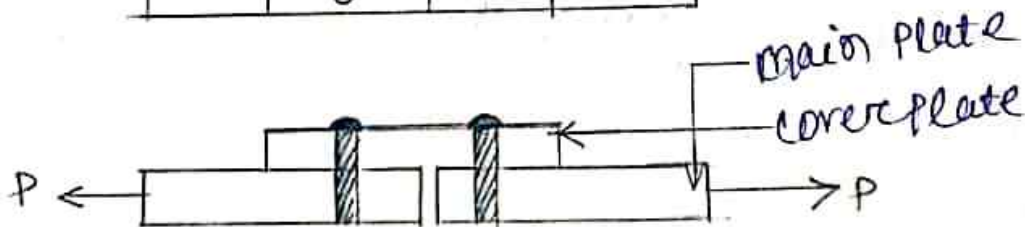
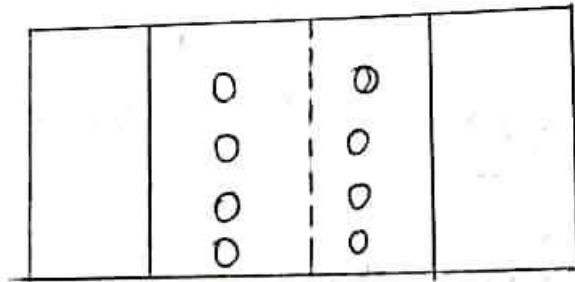


(Double bolted lap joint)

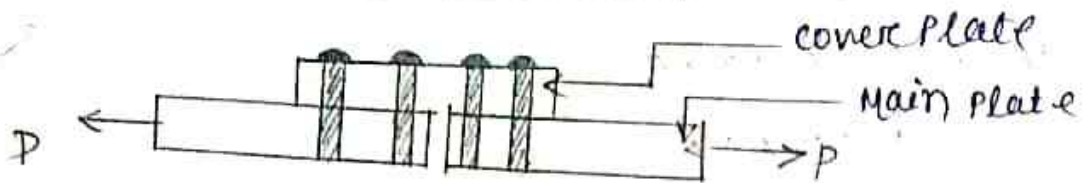
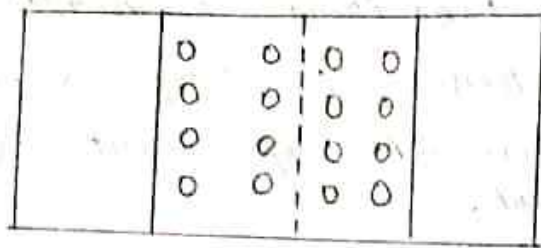
Butt joint

→ The two members ~~are~~ ^{to be} connected ~~are~~ ^{are} placed into either one or both sides, called ~~additional~~ ^{cover} plates, ~~are~~ ^{are} placed and ~~are~~ ^{are} connected to the main plate ~~are~~ ^{as} shown in the figure below.

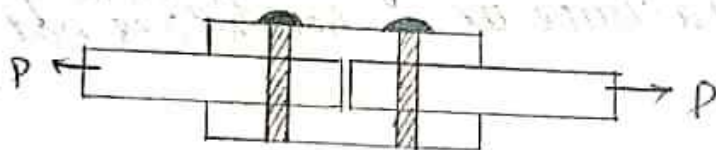
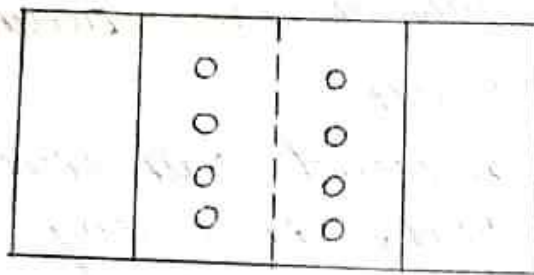
- If the cover plate is provided on one side is called single cover butt joint.
- If the cover plate provided on both sides of the main plate is called double cover butt joint.



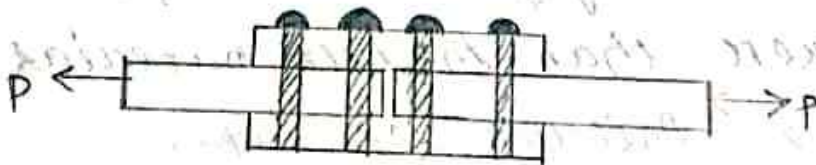
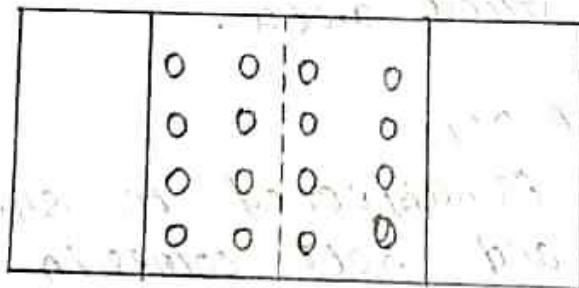
(single cover single bolted butt joint)



(single cover double bolted butt joint)



(double cover single bolted butt joint)



(double cover double bolted butt joint)

NOTE

In case of double cover bolt joint eccentricity of forces does not exist & hence bending is eliminated where as it exists in case of lap joint. That's why cause for bending moment.

Failure of Bolted joint

(1) Shear failure of Bolt

→ Shear stresses are developed when the plates slip due to applied forces. ^{When} the maximum factored shear force in the bolt exceeds the nominal shear capacity of bolt then shear failure of bolts occurred.

(2) Bearing failure of Bolt

→ The bolt is crushed around half circumference. It occurs when the plate is strong in bearing and heaviest stressed plate may press the bolt shank. Bearing failure of bolts ^{generally} does not occur in practice.

(3) Tension failure of Bolt

→ It occurs when the bolt is subjected to tension and may fail at the stress area.

(4) Bearing failure of Plate

→ When an ordinary bolt is subjected to shear forces this slip takes place and bolt comes in contact with the plates. The plate may get crushed, if the plate material is weaker than the bolt material.

(5) Tension or Tearing failure of plates

→ It occurs when the bolts are stronger than plates. during tension.

(B) Block Shear Failure

→ It occurs when the block of material within the bolted area breaks away from the remainder area. The possibility of this failure increases when high strength bolts are used. This type of failure occurs with shear on one plates and tension on perpendicular plane leading to fall of hatched portion of the plate.

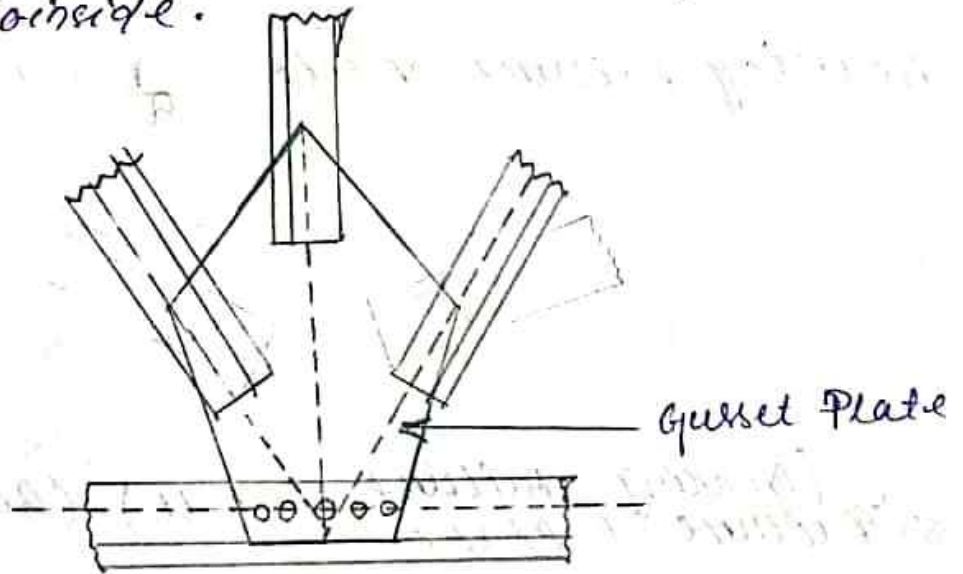
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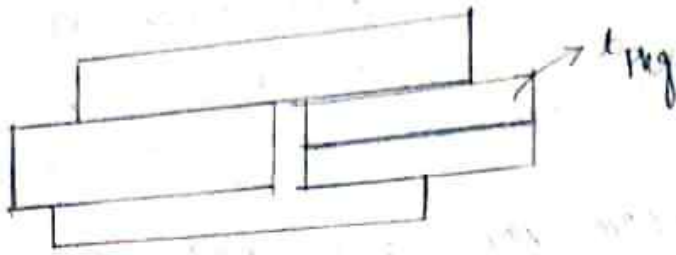
Gusset Plate

→ A gusset plate is a plate provided to make a connection at the place where more than one member is to be jointed.

Ex: ⇒ Joint of truss, guss girder etc

→ The lines of action of truss members meeting at joints are assumed to coincide.





factored (or) Design Bearing strength of bolt (V_{dPb}) $P \rightarrow$ force bearing

$$V_{dPb} = \frac{V_{npb}}{\gamma_{mb}}$$

where,

V_{npb} = Nominal bearing capacity of bolt

$$V_{npb} = 2.5 k_b d t f_u'$$

$$V_{dPb} = \frac{2.5 k_b d t f_u'}{\gamma_{mb}}$$

where,

k_b = Bearing factor

k_b = Smaller of (i) $\frac{e}{3d_0}$ (ii) $\frac{P}{3d_0} - 0.25$ (iii) $\frac{f_{ub}}{f_u}$ (iv) 1.0

$d_0 = d_i$ d = diameter of bolt

e = edge distance

P = Pitch

d_0 = diameter of bolt holes t = thickness of main plate in case of lap joint

f_{ub} = ultimate shear stress of plate t = smaller of (i) thickness of main plate (ii) sum of thickness of cover plate in case of butt joint

t = aggregate thickness of connected plate which experiencing bearing stress in same direction.

f_u' = smaller of f_{ub} & f_u

Spacing of Bolt holes

→ Pitch, ^{edge} distance, end distance define the spacing of bolt holes in a joint

Pitch (P)

- It's distance between the centres of two consecutive bolts measured along a row of bolts. A row generally refers to a line of bolts placed parallel to the forces in a member.
- For wide plates pitch may also be defined as centre to centre (c/c) distance of bolts measured along the length of member or the connection
- When bolts are placed staggered the pitch will be referred to as staggered pitch

Gauge (g)

- It's distance between adjacent bolt lines or the c/c distance between two consecutive bolt measured along the width of the member or connection.
- Gauge lines are also called as bolt line.

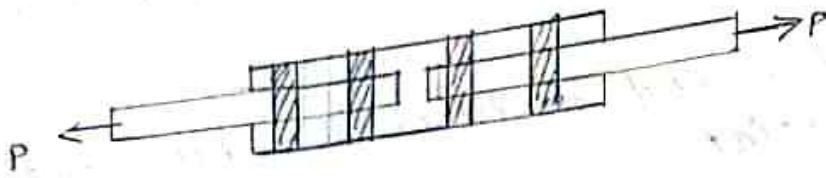
Edge distance

- This is distance at right angle to the direction of forces or stresses from the centre of bolt hole to the adjacent edge of the member. ~~whereas~~

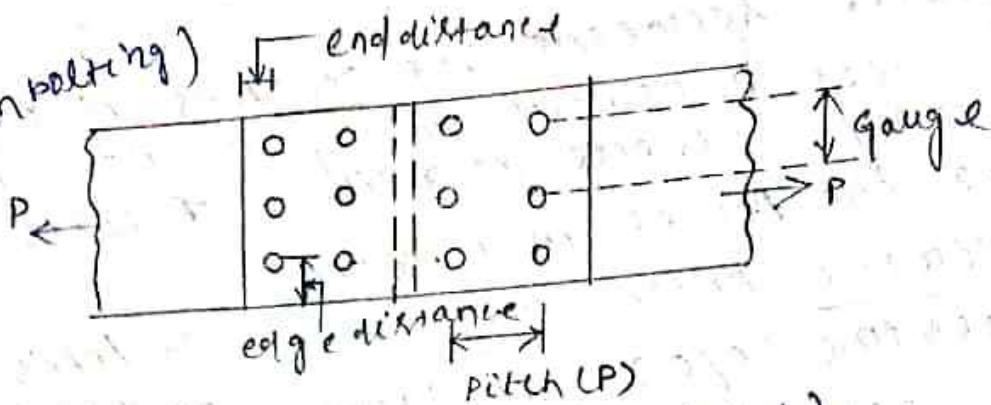
End distance

- This is the distance parallel to the direction of stresses or forces from the centre of bolt hole to the end of the element is called the end distance.

(1)

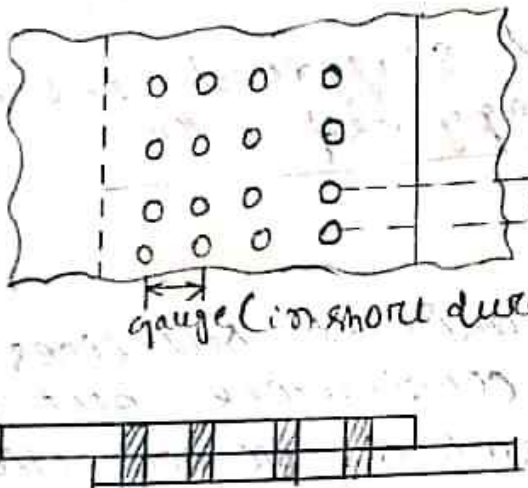


(Chain bolting)



(Double cover butt joint)

(2)



pitch (in long direction)

gauge (in short direction)

(Lap joint with wide plates)

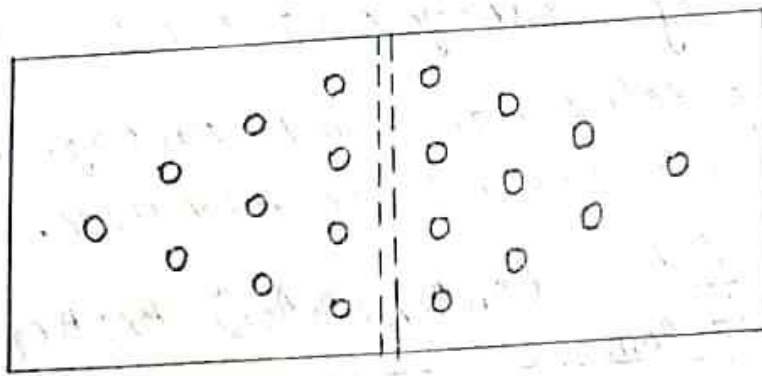
P_1

P_2

P_3

(staggered bolting)

(4)



Double cover butt joint
(Common bolting)

⇒ Packing or stitching bolts are used to make the sections act in unison & to prevent buckling of compression members, when two or more sections are in contact.

⇒ They are not considered in strength calculation. D. 14.01.2020

Factored Design shear strength of bolt (V_{dsb})

$$V_{dsb} = \frac{V_{nsb}}{\gamma_{mb}}$$

where, V_{nsb} = Nominal shear strength of bolt

$$V_{nsb} = \frac{f_{ub}}{\sqrt{3}} (n_n A_{nb} + n_s A_{sb})$$

$$\Rightarrow V_{dsb} = \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} (n_n A_{nb} + n_s A_{sb})$$

where f_{ub} = Ultimate tensile stress

n_n = no. of shear plane with threads intercepting the shear plane.

n_s = no. of shear plane with shank (without threads) intercepting shear plane.

(1.25) γ_{mb} = partial safety factor for bolt material

Again for long joint, grip and package, the above shear strength value will be reduced.

$$V_{dsb} = \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} (\eta_n A_{nb} + A_{sb}) \beta_{lj} \beta_{lg} \beta_{pkg}$$

where,

β_{lj} = A reduction factor to allow the overloading of the end bolts that occur in long joint or connection.

β_{lg} = A reduction factor to allow for the effect of large grip length.

β_{pkg} = A reduction factor to account for packing plates in excess of 6mm

A_{nb} = threaded area or net tensile stress area of bolt

A_{sb} = shank area or nominal shank area

$$A_{nb} = 0.78 A_{sb}$$

(i) Reduction factor for long joint (β_{lj})

→ When $l_j > 15d$ in the direction of load, then the shear capacity is reduced

$$\beta_{lj} = 1.075 - \frac{l_j}{200d}$$

for $0.75 \leq \beta_{lj} \leq 1.0$

where l_j = length of joint & is taken as the distance between first & last row of bolt in a joint measured in the direction of the load transfer.

(ii) Reduction factor for large grip length (β_{lg})

When a grip length of a bolt increases, the bolt is subjected to a greater bending moment due to shear forces acting on its shank. Therefore total thickness (t) is greater than $5d$, then the shear capacity of bolt is reduced.

$t > 5d$ then the shear capacity of bolt is reduced

where,

t = total thickness of connected plate

$$\beta_{lg} = \frac{8d}{3d + l_g}$$

NOTE

$$\left(\begin{array}{l} \beta_{lg} \neq \beta_{ei} \\ \beta_{lg} \neq 8d \end{array} \right)$$

(iii) Reduction factor for packing plate

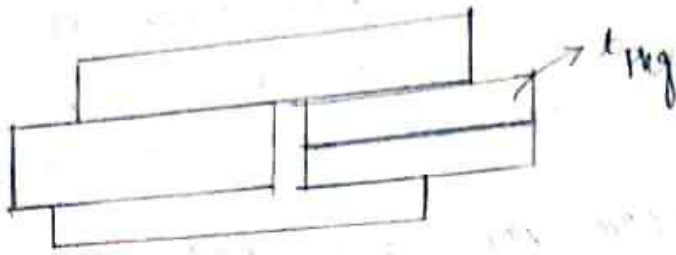
When the packing plate are more than 6mm in thickness, the shank of the bolt is subjected to bending which affect the nominal shear capacity of the bolt by a reduction factor of β_{pkg}

$$\beta_{pkg} = 1 - 0.0125 t_{pkg}$$

when

where, $t_{pkg} > 6\text{mm}$

t_{pkg} = thickness of packing plate



factored (or) Design Bearing strength of bolt (V_{dPb}) $P \rightarrow$ force bearing

$$V_{dPb} = \frac{V_{npb}}{\gamma_{mb}}$$

where,

V_{npb} = Nominal bearing capacity of bolt

$$V_{npb} = 2.5 k_b d t f_u'$$

$$V_{dPb} = \frac{2.5 k_b d t f_u'}{\gamma_{mb}}$$

where,

k_b = Bearing factor

k_b = Smaller of (i) $\frac{e}{3d_0}$ (ii) $\frac{P}{3d_0} - 0.25$ (iii) $\frac{f_{ub}}{f_u}$ (iv) 1.0

$d_0 = d_i$ d = diameter of bolt

e = edge distance

P = Pitch

d_0 = diameter of bolt hole t = thickness of main plate in case of lap joint

f_{ub} = ultimate shear stress of plate t = smaller of (i) thickness of main plate (ii) sum of thickness of cover plate in case of butt joint

t = aggregate thickness of connected plate which experiencing bearing stress in same direction.

f_u' = smaller of f_{ub} & f_u

Factored (or) design tensile strength of bolt (T_{db})

$$T_{db} = \frac{T_{db}}{\gamma_m} = \frac{\text{Nominal (characteristic) tensile strength of bolt}}{\text{Partially safety factor}}$$

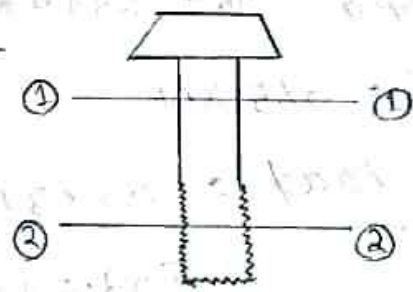
→ Applicable when tensile load is applied on bolt.
 → when a bolt is subjected to factored or design tensile load (T), it make chance to fail by

- (1) Gross section yielding failure
- (2) Net section rupture / fracture (or) brittle fracture failure.

(1) $T_{db1} = \frac{A_{sb} f_y b}{\gamma_{m0}}$ (when bolt fails in yielding)

(2) $T_{db2} = \frac{0.9 A_n f_{ub}}{\gamma_{m1}}$ (when bolt fails in ultimate stress)
 [$A_n = \text{Net rupture area}$] 0.16.01.2020

∴ $T_{db} = \text{least of } T_{db1} \text{ and } T_{db2}$



If failure at ①-① ⇒ It is yielding failure

If failure at ②-② ⇒ It is net section rupture

⇒ Design strength of bolt = Bolt value = least of V_{ds} , V_{db} & T_f (or any)

⇒ No. of bolts required to resist design (or) factored axial load (P_d) =

$$n = \frac{P_d}{V_{db}}$$

NOTE

Assume steel of grade Fe 410 if grade of bolt not specified. Also assume that the threads of bolt pass into the shear planes if not specified, if not specified, $r = 3.8 \text{ mm}$, $p = 50 \text{ mm}$

Ques design

Design a lap joint to connect two plates 300 mm wide 16 mm thick using 20mm diameter bolt of grade A 4.6. the applied service load is 375 kN

Soln

Given data

Lap joint \Rightarrow It's Bolt will be in single shear

width of plate = B = 300 mm
Assume 410 grade plate $\Rightarrow f_u = 410 \text{ MPa}$
thickness of plate = t = 16 mm

diameter of bolt = d = 20 mm

hole dia of bolt = $d_h = d_0$

$= 20 + 2$

$d_h = d + 2$
when d = 16 $\Rightarrow 24 \text{ mm}$

$A_{sb} = \frac{\pi}{4} \times 20^2 = 314 \text{ mm}^2$
4.6 grade bolt $\Rightarrow A_{sb} = 314 \text{ mm}^2$

$f_{ub} = 400 \text{ MPa}$

$A_{nb} = 0.78 \times A_{sb}$
 $= 0.78 \times 314$

$f_{yb} = 400 \times 0.6 = 240 \text{ MPa}$

$A_{nb} = 244 \text{ mm}^2$

Applied service load = P = 375 kN

\Rightarrow Design (or) factored load = 1.5×375

$\gamma_{mb} = 1.25$
 $= 562.5 \text{ kN} = P_d$

(1) Design shear strength of 1 bolt

$V_{dsb} = \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} (n_s A_{nb} + n_b A_{sb})$

Assume end plate intercept thread
 $\Rightarrow n_s = 1, n_b = 0$

$= \frac{400}{\sqrt{3} \times 1.25} (1 \times 244 + 0)$

$\Rightarrow V_{dsb} = 45079.50 \text{ N}$

$e_{min} = 1.7 d_h = 1.7 \times 22 = 37.4 \text{ mm} \approx 50 \text{ mm}$
 $P_{min} = 2.5 d = 2.5 \times 20 = 50 \text{ mm}$

$\Rightarrow V_{dsb} = 45.08 \text{ kN}$

(ii) Design bearing strength of bolt

$$\Rightarrow V_{dpb} = \frac{2.5 k_b d t f_u}{\gamma_{mb}}$$

$$k_b = \text{smallest of (i) } \frac{e}{3d_0} = \frac{40}{3 \times 20} = 0.6$$

$$(ii) \frac{p}{3d_0} = \frac{50}{60} = 0.51$$

$$(iii) \frac{f_{ub}}{f_u} = \frac{400}{410} = 0.97$$

$$(iv) 1.0$$

$$\Rightarrow k_b = 0.51$$

$$\Rightarrow V_{dpb} = \frac{2.5 \times 0.51 \times 20 \times 16 \times 400}{1.25}$$

$$\Rightarrow V_{dpb} = 130560 \text{ N}$$

$$\Rightarrow V_{dpb} = 130.56 \text{ kN}$$

$$T_{db1} = \frac{A_{sv} f_{yb}}{\gamma_{m0}}$$

$$\Rightarrow T_{db1} = \frac{314 \times 240}{1.1}$$

$$\Rightarrow T_{db1} = 68509 \text{ N}$$

$$\Rightarrow T_{db1} = 68.51 \text{ kN}$$

$$T_{db2} = \frac{0.9 A_n f_{ub}}{\gamma_{m2}}$$

$$A_n = (p - n d_h) t$$
$$= (50 - 1 \times 22) \times 16$$

$$= 28 \times 16$$

$$= 448 \text{ mm}^2$$

$$T_{db2} = \frac{0.9 A_n f_{ub}}{\gamma_{m1}}$$

$$= \frac{0.9 \times 148 \times 400}{1.25} = 129024 \text{ N}$$

$$= 129 \text{ kN}$$

$$\Rightarrow T_{db2} = 129 \text{ kN}$$

So, smaller value is taken

$$T_{db1} = 68.51 \text{ kN}$$

$$V_{dcb} = 45.08 \text{ kN}$$

$$V_{dcpb} = 130.56 \text{ kN}$$

\therefore Design strength of bolt = V_{db} = smaller of $V_{dcb}, V_{dcpb}, T_{db}$

$$\Rightarrow V_{db} = V_{dcb} = 45.08 \text{ kN}$$

no. of bolts required to resist factor load 562.5 kN

$$\Rightarrow n = \frac{P_d}{V_{db}}$$

$$= \frac{562.5}{45.08}$$

$$= 12.47 \text{ nos}$$

NOTE

cover plate thickness $\approx 13 \text{ nos}$

for single cover butt joint thickness of cover plate = $1.25 t_{min}$

for double cover butt joint thickness of cover plate = $\frac{5}{8} t_{min}$

Analysis
 Calculate the strength of the ^{20mm} diameter bolt of grade 4.6 for the following cases. The main plates to be jointed are 12mm thick.

(a) lap joint

(b) single cover butt joint, cover plate thickness = 10mm

(c) double cover butt joint, when each of the cover plate being 8mm thick

0.17.01.2020

Given data

diameter of bolt (d) = 20mm

diameter of bolt holes (d_h) = $20 + 2$
 = 22mm

thickness (t) = 12mm

Shank area of bolt

$$A_{sb} = \frac{\pi}{4} \times 20^2$$

Thread area of bolt

$$A_{tb} = 0.78 \times A_{sb}$$

$$= 0.78 \times 314$$

$$\Rightarrow A_{tb} = 245 \text{ mm}^2$$

4.6 grade

$$f_{ub} = 4 \times 100 = 400 \text{ MPa}$$

$$f_{yb} = 400 \times 0.6 = 240 \text{ MPa}$$

Assume Fe 410 grade of steel = $f_u = 410 \text{ MPa}$

$$\gamma_{mb} = 1.25$$

(i) lap joint

The bolt will be in single shear and bearing

design shear strength of bolt

$$V_{dsb} = \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} (n A_{sb} + 3 A_{tb})$$

(Assume shear plane intercept at thread of bolt)
 $\eta_n = 1, \eta_s = 0$

$$V_{dsb} = \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} \quad (\eta_n A_{nb} + \eta_s A_{ns})$$

$$= \frac{400}{\sqrt{3} \times 1.25} \quad (1 \times 295)$$

$$= 45264.26 \text{ N}$$

$$= 45.26 \text{ kN}$$

Design bearing strength of ^{one} bolt

$$V_{dpb} = \frac{2.5 k_b d t f_{ub}}{\gamma_{mb}}$$

Assume Pitch $p = 50 \text{ mm}$, $e = \text{edge distance} = 33$

$$k_b = \text{smaller of (i) } \frac{e \rightarrow 33}{3d_0} = \frac{33}{3 \times 22} = 0.5$$

$$(ii) \frac{p \rightarrow 50}{3d_0} - 0.25 = \frac{50}{3 \times 22} - 0.25 = 0.5$$

$$(iii) \frac{f_{ub}}{f_u} = \frac{400}{410} = 0.97$$

$$(iv) 1.0$$

$$\Rightarrow \boxed{k_b = 0.5}$$

$$V_{dpb} = \frac{2.5 \times 0.5 \times 20 \times 12 \times 400}{1.25}$$

$$= 96000 \text{ N}$$

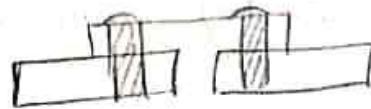
$$= 96 \text{ kN}$$

\therefore The strength of bolt $= V_{db}$

\Rightarrow smaller of V_{dsb} & V_{dpb}

$$\Rightarrow \boxed{V_{dsb} = 45.26 \text{ kN}}$$

(ii) single cover butt joint when cover plate thickness = 10 mm



Bolt will be in single shear.

$$V_{dsb} = \frac{f_{ub}}{1.3 \gamma_{mb}} (\eta_n A_{nb} + \eta_s A_{sb})$$

$$\Rightarrow 45.26 \text{ kN}$$

$$V_{dpb} = \frac{2.5 k_b \times d \times t \times f_{ub}}{\gamma_{mb}}$$

t = thickness of main plate in case of lap joint

t = smaller of (i) thickness of main plate } in case of
 (ii) sum of thickness of cover plate } butt joint

$$V_{dpb} = \frac{2.5 k_b \times d \times t \times f_{ub}}{\gamma_{mb}}$$

$$= \frac{2.5 \times 0.5 \times 20 \times 10 \times 400}{1.25}$$

$$= 80000 \text{ N}$$

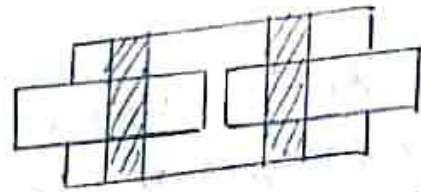
$$\Rightarrow \boxed{V_{dpb} = 80 \text{ kN}}$$

∴ Design strength of bolt in case of single cover butt joint = V_{dps}
 smaller of V_{dsb} & V_{dps}

$$\Rightarrow \boxed{V_{dps} = 45.26 \text{ kN}}$$

$$\boxed{V_{dps} = 45.26 \text{ kN}}$$

(iii) Double cover butt joint, when each of the cover plate being 8mm thick



The bolt will be in double shear and bearing.
 The shear strength of one bolt in double shear V_{dsb}

$$\Rightarrow V_{dsb} = 2 \times \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} (\eta_n A_{nb} + \eta_s A_{ns}) \quad [\because \eta_n = 2, \eta_s = 0]$$

$$\Rightarrow V_{dsb} = 2 \times 15.26$$

$$\Rightarrow \boxed{V_{dsb} = 90.52 \text{ kN}}$$

Design bearing strength of one bolt $V_{dpb} = \frac{2.5 \times k_b \times d \times t \times f_u'}{\gamma_{mb}}$

$$V_{dpb} = \frac{2.5 \times k_b \times d \times t \times f_u'}{\gamma_{mb}} = \frac{2.5 \times 0.5 \times 20 \times 12 \times 400}{1.25}$$

$t =$ smaller of (i) thickness of main plate = 12 mm
 (ii) sum of cover plate thickness = 16 mm
 $t = 12$ (B78)

$$= 96000 \text{ N}$$

$$\Rightarrow \boxed{V_{dpb} = 96 \text{ kN}}$$

\therefore strength of bolt in case of double cover butt joint = smaller of V_{dsb} & V_{dpb}

$$\Rightarrow \boxed{V_{dsp} = 90.52 \text{ kN}}$$

NOTE

→ Design strength of bolt = V_{db} = smaller of V_{dsb} & V_{dph}

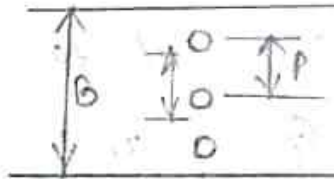
→ No. of bolt required to resist the factored load

$$(P_d) = n = \frac{P_d}{V_{db}}$$

Design bearing (or) tensile strength of plate: - (T_{dp})

$$\eta_{dp} = \frac{\eta_{np}}{\gamma_m} \Rightarrow T_{dp} = \frac{0.9 A_n f_u}{\gamma_{m1}}$$

where, A_n = net rupture area of plate
 $= (B - n d_h) t$
 $= (p - n d_h) t$



0.18.01.2020

NOTE

→ Design strength of bolted connection (or) joint

= least of V'_{dsb} , V'_{dph} & T_{dp}
(smaller)

V'_{dsb} = design shear strength of bolted joints
lap
 $= n \times V_{dsb}$ (n = total no. of bolts in joint)

V'_{dph} = design bearing strength of bolted joint
 $= n \times V_{dph}$ (n = total no. of bolt in one side in case of butt joint)

→ Efficiency of bolted connection (or) joint =

$$\eta = \frac{\text{Design strength of joint}}{\text{Design strength of solid plate } (T_{dsp})} \times 100$$

where $T_{dsp} = \frac{A_g f_y}{\gamma_{m0}}$ ($A_g = B \times t$)
→ thickness of plate.
→ Gross Area

efficiency of bolted connection or joint η (%)
 $\eta (\%) = \frac{\text{Design strength of joint per pitch} \times 100}{\text{Design strength of solid plate per pitch}}$

$$P_{dsb} = \frac{A_g f_y}{\gamma_{mo}} \quad (A_g = p \times t)$$

Ques

Find the maximum force that can be transmitted through a double bolted chain lap joint consisting of 6 bolts in 2 rows. Given that M16 grade bolts in 2 rows are grade 4.6 & plates of Fe 410 are used. The thickness of plate are connected to be taken as 10 mm & 12 mm.

Given data

No. of bolts = $n = 6$

M16 bolt $\Rightarrow d = 16 \text{ mm}$
 \downarrow \rightarrow shank dia. of bolt

Metric

hole dia of bolt = 16.72
 $= 18 \text{ mm}$

Bolt of grade 4.6

$f_{ub} = 4 \times 100 = 400 \text{ MPa}$

$f_{yb} = 400 \times 0.6 = 240 \text{ MPa}$

Plate grade Fe 410 $\Rightarrow f_u = 410 \text{ MPa}$

$t = 10 \text{ mm}$

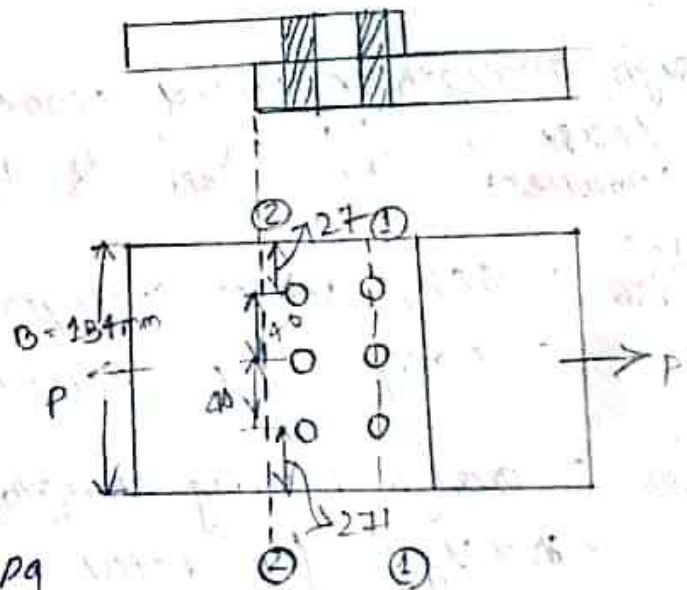
$A_{sb} = \frac{\pi}{4} \times 16^2 = 201 \text{ mm}^2$

$A_{nb} = 0.78 \times A_{sb}$

$= 0.78 \times 201$

$= 157 \text{ mm}^2$

$= 157 \text{ mm}^2$



Maximum force that can be transmitted through this bolted joint.

Strength of joint = Smaller of V'_{dsb} , V'_{dpb} & T_{dp}

$$V'_{dsb} = n \times V_{dsb}$$

$$V'_{dpb} = n \times V_{dpb}$$

$$T_{dp} = \frac{0.9 A_n f_u}{\gamma_m}$$

(i) Lap joint \Rightarrow Bolt will be in single shear
 Design shear strength of 1 bolt

$$V_{dsb} = n \times V_{dsb}$$

$$V_{dsb} = n \times \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} (n_1 A_{nb} + n_2 A_{ns})$$

$$= \frac{400}{\sqrt{3} \times 1.25} (1 \times 157 + 0)$$

$$= 29006.07 \text{ N}$$

$$= 29.01 \text{ kN}$$

$n_n = 1, n_s = 0$
 shear plane intersects thread of the bolt

\Rightarrow Design shear strength of lap joint = $n \times V_{dsb} =$

$$= 6 \times V_{dsb}$$

$$= 6 \times 29.01$$

$$= 174.06 \text{ kN}$$

(ii) Design bearing strength of 1 bolt = V_{dpb}

$$V_{dpb} = \frac{2.5 k_b d t f_u}{\gamma_{mb}}$$

$$\text{Minimum pitch (P)} = 2.5d = 2.5 \times 16 = 40 \text{ mm}$$

$$\text{Minimum end distance} = e = 1.5d_h = 1.5 \times 18$$

$$= 27 \text{ mm}$$

$$k_b = \text{smaller of (1) } \frac{e}{3d_0} = \frac{27}{3 \times 18} = 0.5$$

$$(2) \frac{P}{3d_0} - 0.25 = \frac{40}{3 \times 18} - 0.25 = 0.49$$

$$(3) \frac{f_{ub}}{f_u} = \frac{400}{410} = 0.97$$

$$(4) 1.0$$

$$V_{dPB} = \frac{2.5 k_b d t f_u}{\gamma_{mb}}$$

$$= \frac{2.5 \times 0.49 \times 10 \times 400}{1.25}$$

$$= 627 \text{ kN}$$

∴ design bearing strength of joint = $7 \times V_{dPB}$

$$= 7 \times 627$$

$$= 372 \text{ kN}$$

$$= 376.32 \text{ kN}$$

(3) Design tearing strength of plate

$$P_{dP} = \frac{0.9 A_n f_u}{\gamma_{m1}}$$

∴ width of plate = $b = 2 \times 40 + 2 \times 27$

$$= 134 \text{ mm}$$

At section ①-①

$$A_n = (b - n d_h) t$$

$$= (134 - 3 \times 18) \times 10$$

$$= 80 \times 10 = 800 \text{ mm}^2$$

$$P_{dP} = \frac{0.9 \times 800 \times 410}{1.25} = 236.16 \text{ kN}$$

∴ design strength of material of joint

$$= \text{Lesser of } V'_{dsb}, V'_{dpb} \text{ \& } \tau_{df}$$

$$= 174 \text{ kN}$$

∴ maximum force that can be transmitted = 174 kN
 D. 27. 01. 2020

- state the assumption in design of bearing bolts
- the stress distribution on the plates betwⁿ the bolt hole is uniform.
 - the friction betwⁿ the plate is negligible
 - the shear stress is uniformly distributed over the cross-section of the bolt.
 - the bolts in a group share the direct load equally
 - bending stresses develop in the bolts is neglected.

What are the advantages of butt joint over lap joint

→ there is no eccentricity develop in butt joint & load carrying capacity is higher than lap joint because in lap joint some eccentricity occurs which may cause bending.

→ Butt joint is permanently leak proof and strong

Shear strength of HSBG bolts

$$V_{df} = \frac{V_{HSB}}{\gamma_{mf}} = \frac{M_f n_e k_h F_0}{\gamma_{mf}}$$

where

M_f = slip factor (or) friction co-efficient

n_e = number of interfaces offering frictional resistance to slip

k_h = constant (best) of type of hole

F_0 = proof load ⇒ minimum bolts tension at installation

$$F_0 = f_0 A_{nb}$$

where, f_0 = proof stress

f_0 = Proof stress = $0.7 f_{ub}$

f_{ub} = ultimate tensile stress of bolt

γ_{mf} = 1.1 for slip resistance design at service load
= 1.25 for slip resistance design at ultimate load.

WELDED CONNECTION

Advantages of welded connection over bolted connection

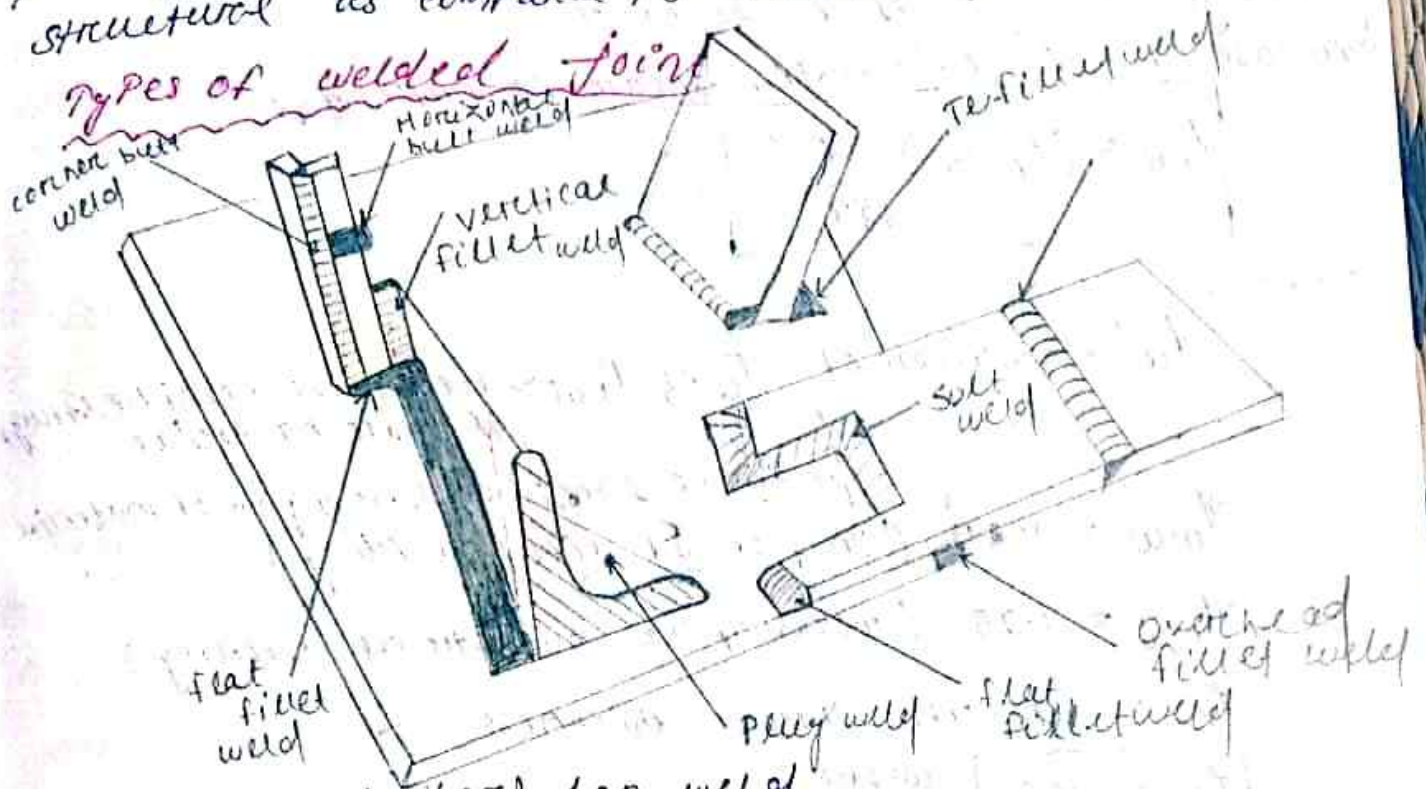
- welded joints are economical because bolt materials are eliminated.
- welded structures are more rigid/compact compare to bolted joint.
- As this joint is rigid joint, moment is less shear force is less, less deflection and less radius of gyration. So 100% efficiency can be achieved by using this joint.
- lighter in weight so less cost.
- Alteration can be done with less expenses in case welding as compare to bolting.
- The process of welding is quicker in comparison between welding...
- The process of welding is silent where as in case of riveting a lot of noise is produced.

Disadvantages

- More skilled person is required to make welded joint as compared to bolted joint.
- The inspection of welded joint is difficult and expensive where as bolted joints can be inspected simply by tapping a joint with a hammer.
- Welded structures are brittle in nature so under dynamic load, welded connection is first fail then bolted connection.

→ fatigue is less of a welded structure
 → fatigue strength is less in case of welded structural as compare to bolted connection.

Types of welded joint

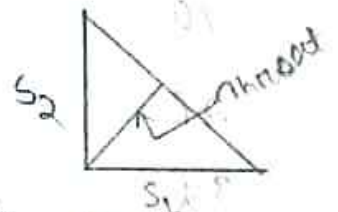
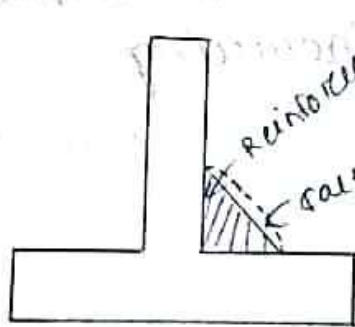


- (i) Fillet weld (or) Lap weld
- (ii) Groove weld (or) butt weld
- (iii) Plug and slot weld

(i) Fillet weld (or) lap weld

It is provided when fusion faces are perpendicular in two different plane.

Typical cross-section of fillet weld,



NOTE

- (1) Standard cross-section of Lap weld = Right angle triangle.
- (2) Standard angle for fillet weld section = 45°
- (3) Fillet weld symbol =
- (4) Fillet welds are effective in resisting the shear stresses.

(5) Throat of fillet weld is weakest section of fillet weld.

(6) Design strength of fillet weld
In case of fillet weld, shear is critical

$$P_{dw} = (t_e l_w) \frac{f_u'}{\sqrt{3} \gamma_{mw}}$$

where,

f_u' = smaller of f_u & f_{uw} → ultimate tensile strength of plate material

↓
ultimate tensile strength of material

$\gamma_{mw} = 1.25$ (in case of field welding)

$\gamma_{mw} = 1.5$ (workshop (or) industrial welding)

t_e = effective throat thickness

$$t_e = k s \quad \text{where } s = \text{size of weld}$$

Angle between fusion faces	60-90	91-100	101-106	107-113	114-120
k	0.7	0.65	0.6	0.55	0.5

Minimum size of weld

0.28.01.2020

	Thickness of the thicker plate	S_{min} (mm)
Above	up to s including	
0	10	3
10	20	5
20	32	6
32	50	8 (1st run) 10 (2nd run)

Maximum size of the weld (ϕ Smax) ^{rounded} edges

$$S_{max} = \frac{3}{4} \times t_{min} = 0.75 t_{min} \quad (\text{for } \text{rounded} \text{ edges})$$

$$S_{max} = t_{min} - \phi 1.5 \quad (\text{for } \text{square} \text{ edges})$$

t_{min} = minimum thickness of the plate thinner connected member

$t_e L_w$ = effective Area (A_e)

$$L_w = \text{effective length of weld} = L_w - 2S$$

L_w = overall length of weld

$2S$ = end return

End return

→ An excess ^{length} of the weld on the L arc case for a length of $2S$ is provided to avoid ^{the} initiation of failure from the edge. This is known as end return.

→ This provision applies in the particularly fillet weld in tension.

Reduction ^{Factor} for long joint

if $L_j > 150 t_e$ then $\beta_{ej} = 1.2 - \frac{0.2 L_j}{150 t_e}$

$$\boxed{\beta_{ej} \leq 1}$$

L_j = length of side fillet weld parallel to the direction of a load in a member

$$\boxed{P_{dw} = (t_e \cdot L_w) \frac{f_u'}{\sqrt{3} \gamma_{mw}} \times \beta_{ej}}$$

Specification for fillet weld

→ length of a parallel weld on each side should ^{not} be less than B (width of a plate)

$$L_{\text{parallel}} \neq B$$

→ effective length of weld should not be less than t_s

$$l_w \neq t_s \text{ (or) } 40 \text{ mm}$$

(whichever is less)

→ $l_o \neq 4t$ (or) 40 mm
(whichever is more)

l_o = overlap length of weld

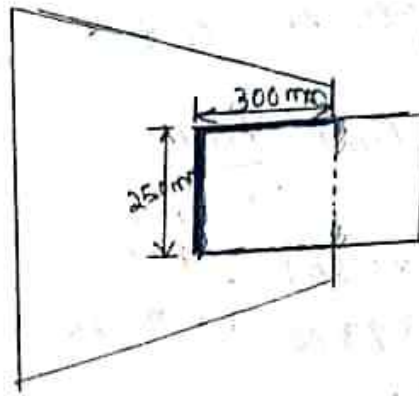
t = thickness of thinner connected member.

→ $B \neq 16t$

If $B > 16t$, slot & plug weld are provided

Ques-1 Design a welded lap joint for two plates of size $120 \text{ mm} \times 8 \text{ mm}$ & $120 \text{ mm} \times 12 \text{ mm}$ for maximum efficiency. Assume shop welding and Fe 410 grade of steel.

Ques-2 A tie member in a truss girder is $250 \text{ mm} \times 14 \text{ mm}$ in size. It is welded to a 10 mm thick gusset plate by a fillet weld. The overlap of the member is 300 mm & weld size is 6 mm . Determine the design strength of joint, if the welding is done as shown in the fig. What is the increase in strength of joint, if the welding is done all around. Assume shop welding.



Given data

Fe 410 grade steel

$$f_u = 410 \text{ MPa}, f_y = 250 \text{ MPa}$$

shop weld, $\eta_{mw} = 1.25$

effective length of weld, $l_w = 2 \times 300 + 250 = 850 \text{ mm}$

effective throat thickness = $t_t = k_s$
 $= 0.7 \times s$

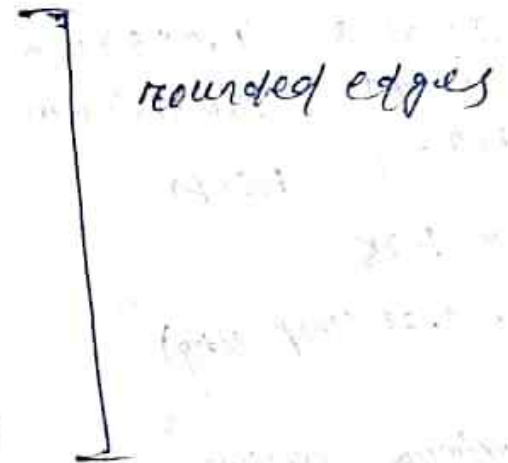
$$s_{\min} = 5 \text{ mm}$$

$$s_{\max} = \frac{3}{4} \times t_{\min}$$

$$= \frac{3}{4} \times 10$$

$$= 7.5$$

\therefore size of weld = 8 mm



$$t_t = k_s$$

$$= 0.7 \times s$$

$$= 4.2$$

Solution

$$P_{dw} = (t_t + l_w) \frac{f_u}{\sqrt{3} \eta_{mw}}$$

$$= (4.2 \times 850) \times \frac{410}{\sqrt{3} \times 1.25}$$

$$= 676059 \text{ N}$$

$$\Rightarrow P_{dw} = 676 \text{ kN}$$

When welding is done all around

$$\text{effective length of weld} = l_w = 2 \times 300 + 2 \times 250 = 1100 \text{ mm}$$

$$P_{dw} = (t_p l_w) \frac{f_{yw}}{\sqrt{3} \times 1.25}$$

$$= (4.2 \times 1100) \frac{410}{\sqrt{3} \times 1.25}$$

$$= 874893 \text{ N}$$

$$= 874. \text{ KN}$$

∴ Increase in strength of weld = 874 - 676 = 198 KN

Q. 1 D. 29.01.2020

Design a welded lap joint for two plates of size 120mm x 8mm and 120mm x 12mm for maximum efficiency. Assume shop welding and Fe 410 grade of steel.

Given data

2 plates (120 x 8) mm

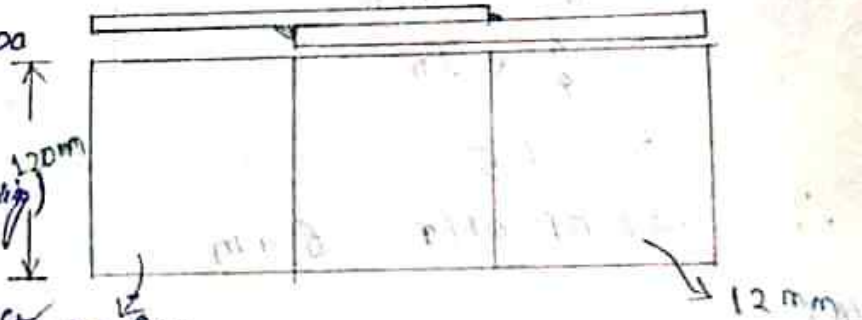
$f_y = 250 \text{ MPa}$ (120 x 12) mm

Fe 410 $\Rightarrow f_u = 410 \text{ MPa}$

$$\gamma_{m1} = 1.25$$

$$\gamma_{mw} = 1.25 \text{ (shop welding)}$$

Sold



For maximum efficiency, $\eta = 100\%$

$$\eta = \frac{\text{Design strength of joint}}{\text{Design strength of solid plate welded}} \times 100$$

$$\Rightarrow 100\% = \frac{\text{Design strength of joint}}{\text{Design strength of solid plate}} \times 100$$

$$\Rightarrow \text{Design strength of joint} = \text{Design strength of solid plate}$$

$$\begin{aligned} \text{design strength of solid plate} &= T_{dsp} = A_g \frac{f_y}{\gamma_{m0}} \\ &= (120 \times 8) \frac{250}{1.1} \\ &= 218181.82 \text{ N} \\ &= 218.18 \text{ kN} \end{aligned}$$

$$\text{design strength of welded joint} = P_{dw} = (l_w t_f) \frac{f_u}{\sqrt{3} \gamma_{mw}}$$

for maximum efficiency = .

$$\Rightarrow \boxed{P_{dw} = 218.2 \text{ kN}}$$

$$t_f = 8 \text{ S}$$

$$K = 0.7$$

$$S_{min} = 5 \text{ min}$$

$$S_{max} = 8 - 1.5$$

$$= 6.5 \text{ mm}$$

$$\therefore S = 6 \text{ mm}$$

$$t_f = K S$$

$$= 0.7 \times 6$$

$$\Rightarrow \boxed{t_f = 4.2}$$

$$\Rightarrow P_{dw} \Rightarrow (l_w t_f) \frac{f_u}{\sqrt{3} \gamma_{mw}} = 218.2 \times 10^3$$

$$\Rightarrow P_{dw} \Rightarrow (l_w \times 4.2) \frac{410}{\sqrt{3} \times 1.25} = 218.2 \times 10^3$$

$$\Rightarrow P_{dw} \Rightarrow (l_w \times 4.2) \times 189.37 = 218.2 \times 10^3$$

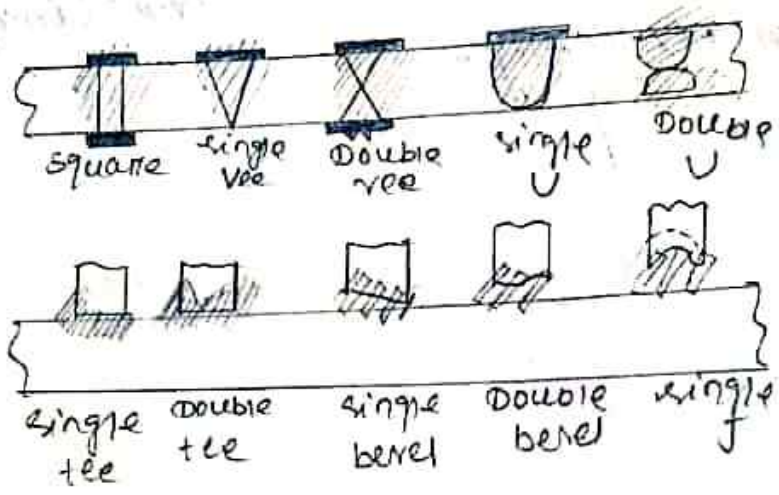
$$\Rightarrow P_{dw} \Rightarrow l_w = 795.35 = 218.2 \times 10^3$$

$$\Rightarrow \boxed{l_w = 274.34 \text{ kN}}$$

lap welded joint will be done at both top & bottom,

$$274.32 \rightarrow l$$

Butt weld (or) Groove weld
 → This type of joint is usually design for direct tension, compression and shear also. but they are design for axial stresses for only under concentric or axial load.



NOTE

→ Butt weld connection is free from eccentricity
 → Butt ^{weld} fails only due to axial stresses.

1) Design axial strength of butt weld (or) Design strength of butt weld :-

$$P_{dw} = (l_w t_e) \left(\frac{f_y'}{\gamma_{mw}} \right)$$

where,

- f_y' = Smaller of yield stress of weld (f_{yw}) and yield stress of parent material (f_y)
- t_e = Effective throat thickness
- l_w = Effective length of weld.

Q) Design shear strength of butt weld (V_{dw}) (or any)

$$V_{dw} = (L_w t_e) \frac{f_y'}{\sqrt{3} \gamma_{mw}}$$

Size of Butt Weld

Size of butt weld specified by throat dimension, is called effective throat thickness (t_e)

$$t_e = \frac{5}{8} t$$

(For single weld, partially penetrated weld like single vee, single U, single J weld etc.)

$$t_e = t$$

(For double V, U weld; fully penetrated weld)

Problem

Two plates of 16 mm and 14 mm thickness are to be joint by a groove weld. The joint is subjected to a factored tensile force of 430 kN. Due to some reasons the effective length of weld that could be provided was 175 mm only. Check the safety of the joint, if

(a) single V groove weld is provided

(b) Double V groove weld is provided

Assume the plate should be shop weld.

Solⁿ

Given data

Two plates, thickness = 16 mm & 14 mm

factored tensile force = 430 kN = P = T_d

Assume Fe 250 grade steel

$f_u = 410 \text{ MPa}$, shop weld $\Rightarrow \gamma_{mw} = 1.25$

$f_y = 250 \text{ MPa}$

Effective length of weld $= l_w = 175 \text{ mm}$

(a) Single-V groove weld is provided

$$t = 14 \text{ mm}$$

$$t_e = \frac{5}{8} t$$

$$= \frac{5}{8} \times 14$$

$$\Rightarrow t_e = 8.75 \text{ mm}$$

Always single V weld is treated as a partially penetrated weld.
 t_e = effective throat thickness
 t = thickness of thinner plate.

Design axial tensile strength of butt weld

$$P_{dw} = (l_w t_e) \left(\frac{f_y}{\gamma_{mw}} \right)$$

$$= (175 \times 8.75) \left(\frac{250}{1.25} \right)$$

$$= 306250 \text{ N}$$

$$\Rightarrow P_{dw} = 306.25 \text{ kN} < 430$$

\therefore So, it is unsafe on which is inadequate.

(b) Double-V groove weld is provided

Effective throat thickness (t_e) = thickness of thinner plate

$$t_e = t$$

$$t_e = 14 \text{ mm}$$

Design axial tensile strength of butt weld

$$P_{dw} = (l_w t_e) \left(\frac{f_y}{\gamma_{mw}} \right)$$

$$= (175 \times 14) \left(\frac{250}{1.25} \right)$$

$$\Rightarrow P_{dw} = 490 \text{ kN} < 430$$

\therefore So, it is safe (or) which is adequate.

Tension Members

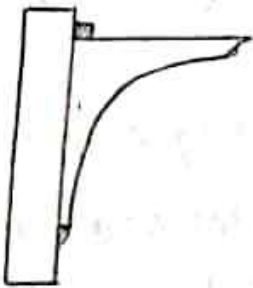
A structural member subjected to two pulling tensile forces applied at its ends is called tension member. The member & connections are arranged that eccentricity in the connection & bending stresses on the member are not developed.

Example of tension joint

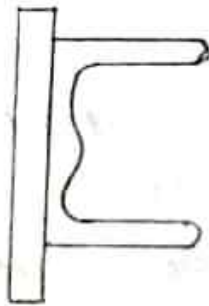
- (i) wire & cable, (ii) bars & rods (iii) ties (iv) plates & flat bars.

Common shapes of tension member

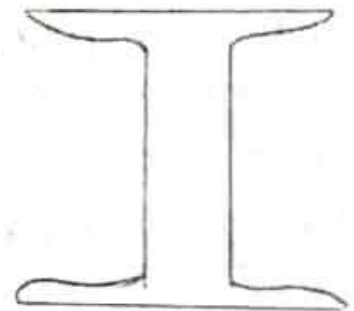
- > open section such as angle, channel & t-section.
- > closed section such as circular, square, rectangular, & hollow section.
- > compound & up sections such as double angle double channel with or without additional plates.



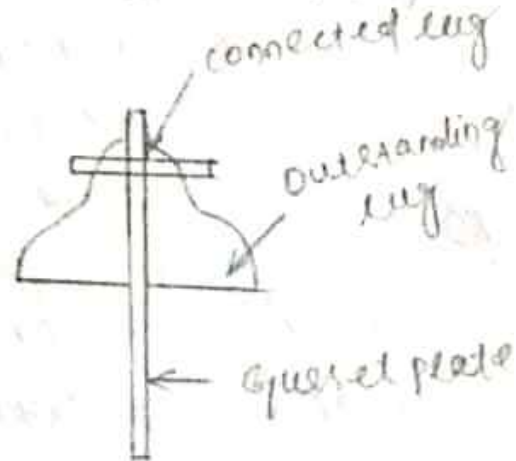
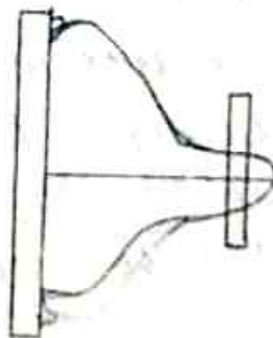
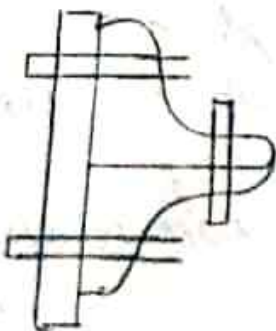
(open section)



(closed section)



(I-section)



Types of failure in tension member

A tension member is subjected to factored or design tension load may change to fail by 3 possible modes. (1) Due to yielding failure.

- (1) Gross section yielding failure.
- (2) Net section rupture failure (tearing or fracture failure)
- (3) Block shear failure.

10.06.02.2020

NOTE

→ If a flat is connected by a single row of bolts the various possible failure are: Gross section yielding & Net section rupture failure.

→ If a flat is connected by two rows of bolts, the various possible failure are gross section yielding failure, Net section rupture failure & block shear failure.

→ If an angle section is connected by a single row of ~~column~~ bolt, the various possible failure are yielding, rupture & block shear failure.

→ If an angle section is connected by two rows of bolts, the various possible failure are yielding, rupture & block shear failure in two ways.

→ In tension member generally Flat section is best & angle section longer leg connected to plate is most suitable for tension case of reversal load.

Design strength of tensile member

(1) Due to gross section yielding (T_{dg})

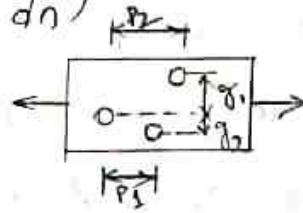
$$T_{dg} = \frac{A_g f_y}{\gamma_{m0}}$$

where, A_g = Gross area = $B \times t$

(2) Due to net section rupture (T_{dn})

(a) For flats & plates

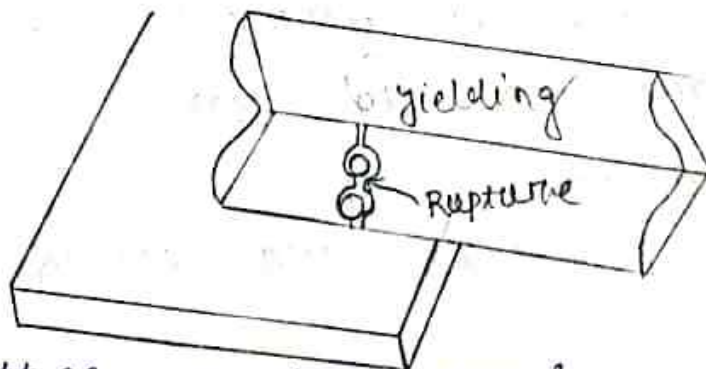
$$T_{dn} = \frac{0.9 A_n f_u}{\gamma_{m1}}$$



$A_n = (B - nd_h) t$ (For chain pattern bolting)

$A_n = \left[B - nd_h + \frac{P_1^2}{4g_1} + \frac{P_2^2}{4g_2} + \dots \right]$ (For staggered pattern bolting)

(b) For angle, tee section, channel section etc



$T_{dn} =$ (strength of connected leg in net section rupture) + (strength of outstanding leg in gross-section yielding)

$$T_{dn} = \frac{0.9 A_{nc} f_u}{\gamma_{m1}} + \frac{\beta A_{go} f_y}{\gamma_{m0}}$$

where,

A_{nc} = connected net area

β = shear lag factor

A_{go} = gross area of the outstanding leg

$$\beta = 1.4 - 0.076 \left(\frac{w}{t} \right) \left(\frac{f_y}{f_u} \right) \left(\frac{b_c}{L_c} \right)$$

w = width of the outstanding leg

b_s = shear lag width

L_c = length of end connection, that is the distance between the outermost bolts in the end joint measured along the load direction or length of the weld along the load direction.

For preliminary design, the rupture strength of net section may be approximately taken as:

$$T_{dn} = \alpha A_n f_u \gamma_{m1}$$

where,

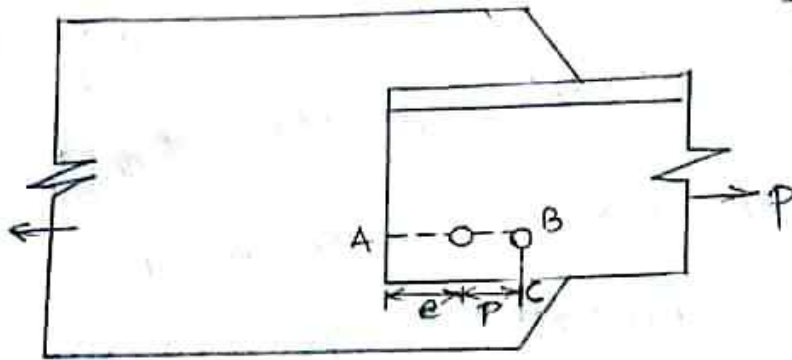
$\alpha = 0.6$ for one two bolts, 0.7 for three bolts & 0.9 for four or more bolts along the length in the end connection or equivalent weld length.

t = thickness of leg

A_n = net area of total cross section.

3) Due to Block Shear (T_{db})

AB = Shear plane
BC = tension plane



$$T_{db1} = \left[\frac{A_{vg} f_y}{\sqrt{3} \gamma_{m0}} + \frac{0.9 A_{tn} f_u}{\gamma_{m1}} \right]$$

$$T_{db2} = \left[\frac{0.9 A_{vn} f_u}{\sqrt{3} \gamma_{m1}} + \frac{A_{tg} f_y}{\gamma_{m0}} \right]$$

Where,

A_{vg}, A_{vn}, A_{tg} = Minimum gross & minimum net sectional area of shear planes respectively

A_{tn}, A_{tn} = Minimum gross & net area sectional area of tension planes respectively

$\therefore T_{db} = \text{Smaller of } T_{db1} \text{ \& } T_{db2}$

$$A_{vg} = (e + P) t \times 2$$

$$A_{vn} = \left[(e + P - d_b - \frac{d_b}{4}) t \right] \times 2$$

$$A_{tg} = P \times t$$

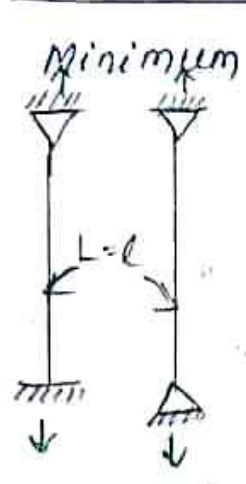
$$A_{tn} = \left[P \times t - \left(\frac{d_h}{4} + \frac{d_h}{4} \right) \times t \right]$$

\therefore Design strength of a tension member
= ~~least~~ ^{smaller} of T_{dg}, T_{dn} & T_{db}

Maximum values of slenderness ratio (λ_{max}) of

$$\lambda = \frac{\text{effective length of tension member (L)}}{\text{minimum radius of gyration } (r_{min})}$$

$$= \frac{\text{unsupported length of tension member (L)}}{\text{minimum radius of gyration } (r_{min})}$$



Minimum radius of gyration (r_{min})

$$r_{min} = \sqrt{\frac{I_{min}}{A}}$$

Member

λ_{max} (or) λ_{limit}

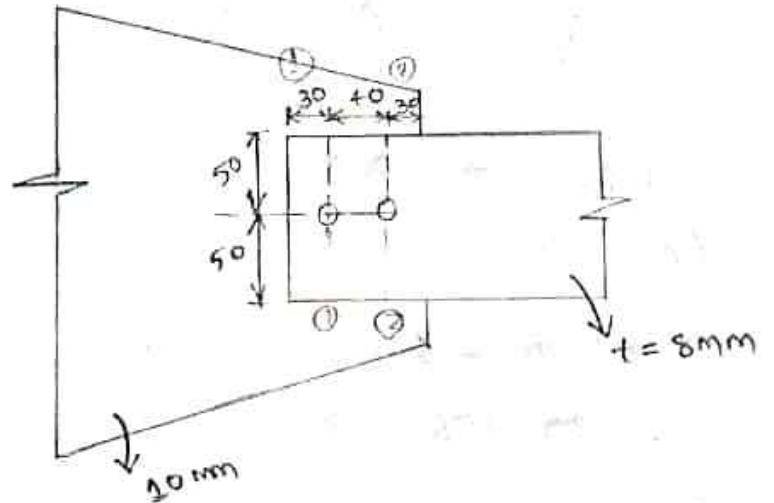
- (i) If a tension member is subjected to reversal of direct stresses / loads due to loads other than wind (or) seismic forces 180
- (ii) If a tension member (in roof trusses & bracing system) subjected to reversal of stresses due to the effect of wind (or) seismic forces. 350
- (iii) If any other tension member (other than pretensioned members) 400

problem

D.11.02.2020

Q1

A tension member consist of a flat 100mm x 8mm which is connected to a gusset plate of 10mm thick by two numbers 16mm dia bolt. As shown in fig. Determine the strength of the flat against yielding, rupture & block shear. Also determine the maximum load the joint can carry safely. Assume steel of grade Fe 410 & bearing bolts of property class 4.6 in the field



Given data

Width of flat = $B = 100\text{mm}$

thickness of flat = $t = 8\text{mm}$

Gusset plate thickness = 10mm

2 no. of 16mm dia.

$$d = 16\text{mm} \Rightarrow d_h = 16 + 2 = 18\text{mm}$$

$$Fe\ 410 \Rightarrow F_{u2} = 410 \frac{\text{N}}{\text{mm}^2}$$

$$f_y = 250 \frac{\text{N}}{\text{mm}^2}$$

$$\text{property class} = 4.6 \Rightarrow f_{ub} = 400\text{MPa}$$

$$f_{yb} = 0.6 \times 400 = 240\text{MPa}$$

Q1

$$A_{n0} = \frac{\pi}{4} \times 10^2 = 201$$

(i) Design strength of flat against yielding

$$T_{dy} = \frac{A_g f_y}{\gamma_{m0}} = \frac{(B \times t) \times f_y}{\gamma_{m0}} = \frac{(100 \times 8) \times 250}{1.1}$$

$$T_{dy} = 181818.18 \text{ N}$$

$$\Rightarrow T_{dy} = 181.82 \text{ kN}$$

(ii) Design the strength of the flat against rupture

$$T_{dn} = \frac{0.9 A_n f_u}{\gamma_{m1}}$$

$$d_h = 18 \text{ mm}$$

$$A_n = (B - n d_h) t$$

$$= (100 - 1 \times 18) \times 8 \quad [\because n = 1]$$

$$= 656 \text{ mm}^2$$

$$T_{dn} = \frac{0.9 A_n f_u}{\gamma_{m1}} = \frac{0.9 \times 656 \times 410}{1.25}$$

$$= \frac{0.9 \times 656 \times 410}{1.25}$$

$$= 193651.2 \text{ N}$$

$$\Rightarrow T_{dn} = 193.65 \text{ kN}$$

(iii) Design strength of flat against Block shear:-

$$T_{db1} = \left[\frac{A_{vg} f_y}{\sqrt{3} \gamma_{m0}} + \frac{0.9 A_{tn} f_u}{\gamma_{m1}} \right]$$

$$T_{db2} = \left[\frac{A_{t2} f_y}{\gamma_{m0}} + \frac{0.9 A_{vn} f_u}{\sqrt{3} \gamma_{m1}} \right]$$

$$A_{lg} = (40 \times 100) \cdot 8$$

$$A_{lg} = (40) \cdot 8 = 320 \text{ mm}^2 \Rightarrow \boxed{A_{lg} = 320 \text{ mm}^2}$$

$$A_{ln} = P \cdot t - \left(\frac{d_h}{4} + \frac{d_n}{4} \right) \cdot t$$

$$= 40 \times 8 - \left(\frac{18}{4} + \frac{18}{4} \right) \times 8$$

$$\Rightarrow \boxed{A_{ln} = 248 \text{ mm}^2}$$

$$\Rightarrow A_{vg} = [(e + p) \cdot t] \times 2$$

$$= [(30 + 40) \cdot 8] \times 2$$

$$\Rightarrow \boxed{A_{vg} = 1120 \text{ mm}^2}$$

$$A_{vn} = \left[(e + p - d_h - \frac{d_h}{4}) \cdot t \right] \times 2$$

$$= \left[(30 + 40 - 18 - \frac{18}{4}) \times 8 \right] \times 2$$

$$\Rightarrow \boxed{A_{vn} = 760 \text{ mm}^2}$$

$$T_{db1} = \left[\frac{A_{vg} f_y}{\sqrt{3} \gamma_{m0}} + \frac{0.9 A_{ln} f_u}{\gamma_{m1}} \right]$$

$$= \left[\frac{1120 \times 250}{\sqrt{3} \times 1.1} + \frac{0.9 \times 248 \times 410}{1.25} \right]$$

$$= 220171.48 \text{ kN}$$

$$\Rightarrow \boxed{T_{db1} = 220.17 \text{ kN}}$$

$$T_{db2} = \left[\frac{A_g f_y}{\gamma_{m0}} + \frac{0.9 n_k n_{fe}}{\sqrt{3} \gamma_{m1}} \right]$$

$$= \left[\frac{320 \times 250}{1.1} + \frac{0.9 \times 160 \times 410}{\sqrt{3} \times 1.25} \right]$$

$$= \cancel{297079.27 \text{ N}} = 202256.26 \text{ N}$$

$$\Rightarrow T_{db2} = \cancel{297 \text{ kN}} \Rightarrow T_{db2} = 202.25 \text{ kN}$$

$\therefore T_{db} = \text{smaller of } T_{db1} \text{ \& } T_{db2}$

$$\Rightarrow T_{db} = 202.25 \text{ kN}$$

Design strength of tension member = smaller of T_{dg} , T_{cn} & T_{db}

\therefore Design strength of tension member = T_{dg}
 = 181.82 kN

Determine the maximum load of the joint can carry

(i) Shear strength of 1 bolt = $V_{dsb} = \frac{f_u}{\sqrt{3} \gamma_{mb}} (n A_{nb} + n_{ps} A_{ps})$ Safety:

$$= \frac{400}{\sqrt{3} \times 1.25} (0 + 1 \times 201)$$

$$= 37135.17 \text{ N} = 37.13 \text{ kN}$$

\Rightarrow shear strength of joint $V_{dsb} = 2 \times 37.13 = 74.26 \text{ kN}$

(ii) Bearing strength of 1 Bolt

$$V_{dpb} = \frac{2.5 k_b d t f_u}{\gamma_{m1}}$$

$k_b = \text{smaller of}$

$$(i) \frac{e}{3d_0} = \frac{30}{3 \times 18} = \frac{5}{9} = 0.54$$

$$(ii) \frac{p}{3d_0} = 0.25 = \frac{40}{3 \times 18} - 0.25 = 0.49$$

D.13.02.2020
1st half

CA-05

STEEL COLUMN BASES & FOUNDATIONS

Design compressive stress in a concrete footing is much smaller than it is in a steel column, so it is necessary to distribute the load from steel column and evenly to the footing below.

Types of Column Bases

- 1) Slab base
- 2) Gusset base
- 3) Grillage foundation

(1) Slab Base

Suitability

- It is most suitable for the column subjected to axial load.
- It is suitable for column subjected to light or less intensity of loads.
- A slab base is assumed to be hinged (pinned) base which can not resist lateral load.

D.13.02.2020

NOTE

Design bearing strength of concrete = $0.45 f_{ck}$

~~Formula for slab base~~

$$A_{nb} = 0.78 A_{sb} \\ = 0.78 \times \frac{\pi}{4} \times 20^2 \\ = 245$$

Design strength against yielding = $T_{dg} = T_d$

$$\Rightarrow \frac{A_g f_y}{\gamma_{m0}} = T_d$$

$$\Rightarrow \frac{A_g \times 250}{1.1} = 225 \times 10^3 \text{ N}$$

$$\Rightarrow 250 A_g = 247500$$

$$A_g = 990 \text{ mm}^2$$

$$\Rightarrow \boxed{A_g = 9.9 \text{ cm}^2}$$

Let us check the section ISA (100 x 75 x 6) mm

Shear strength of one bolt in single shear = V_{dsb}

$$V_{dsb} = \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} (n_n A_{nb} + n_s A_{sb})$$

$$\Rightarrow V_{dsb} = \frac{400}{\sqrt{3} \times 1.25} (1 \times 245 + 0)$$

$$\Rightarrow V_{dsb} = 45264.26 \text{ N}$$

$$\Rightarrow \boxed{V_{dsb} = 45.26 \text{ kN}}$$

Bearing strength of one bolt = $V_{dpb} = \frac{2.5 k_b d t f_u}{\gamma_{mb}}$

Assume $e = 33$, $P = 60$

$$\Rightarrow k_b \text{ smallest of (i) } \frac{e}{2d_0} = \frac{33}{3 \times 22} = 0.5$$

$$(ii) \frac{P}{3d_0} - 0.25 = \frac{60}{3 \times 22} - 0.25 = 0.66$$

$$(iii) \frac{f_{ub}}{f_u} = \frac{400}{410} = 0.97$$

$$(iv) 1.0$$

$$\boxed{k_b = 0.5}$$

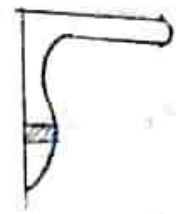
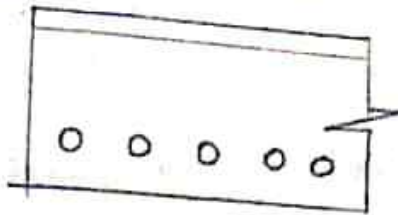
$$V_{dpb} = \frac{2.5 \times 0.5 \times 20 \times 8 \times 400}{1.25} = 64000 \text{ N} \\ \Rightarrow \boxed{V_{dpb} = 64 \text{ kN}}$$

$$V_{dpp} = \frac{2.5 \times 0.5 \times 20 \times 6 \times 400}{1.25} = 48000 \text{ N} \Rightarrow \boxed{V_{dpp} = 48 \text{ kN}}$$

∴ Design strength of bolt = smaller of V_{dsh} & V_{dps}

∴ Design strength of bolt = 48.26 kN

No. of bolt required to resist the factored tensile force (225 kN) = $\frac{225}{48.26} = 4.67 \approx 5$ bolts.



Check

$$A_g = 13.36 \text{ cm}^2 = 1336 \text{ mm}^2$$

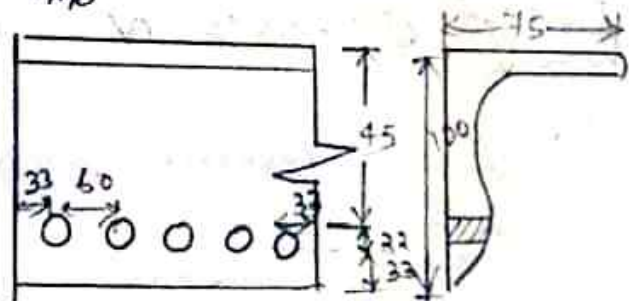
(1) Strength against yield = $T_{dy} = \frac{A_g f_y}{\gamma_{mo}} = \frac{1336 \times 250}{1.1}$

$$\boxed{T_{dy} = 303636.36 \text{ N}}$$

$$\boxed{T_{dy} = 303.63 \text{ kN} > 225 \text{ kN}}$$

(2) Design strength against net section rupture = T_{dn}

$$T_{dn} = \frac{0.9 A_{nc} f_u}{\gamma_{m1}} + \frac{\beta A_{go} f_y}{\gamma_{m0}}$$



$$A_{nc} = (100 - 22 - \frac{8}{2}) 8 = 592 \text{ mm}^2$$

$$A_{go} = (75 - \frac{8}{2}) 8 = 568 \text{ mm}^2$$

$$\beta = 1.4 - 0.076 \left(\frac{w}{t} \right) \left(\frac{f_y}{f_u} \right) \left(\frac{b_s}{L_c} \right)$$

$$b_s = w + w_1 - t = 75 + 95 - 8 = 112 \text{ mm}$$

$$L_c = 33 + 60 + 60 + 60 + 60 - (5 \times 22) = 163 \text{ mm}$$

$$\beta = 1.4 - 0.076 \left(\frac{75}{8} \right) \left(\frac{250}{410} \right) \left(\frac{112}{163} \right)$$

$$\Rightarrow \boxed{\beta = 1.1}$$



$$T_{dn} = \frac{0.9 A_n f_u}{\gamma_{m1}} + \frac{\beta A_g f_y}{\gamma_{m0}}$$

$$= \frac{0.9 \times 592 \times 410}{1.25} + \frac{1.1 \times 568 \times 250}{1.1}$$

$$= 316758.4 \text{ N}$$

$$\Rightarrow T_{dn} = 316.76 \text{ kN} > 225 \text{ kN. (So safe)}$$

Strength against block shear

$$T_{db1} = \frac{A_{vg} f_y}{\sqrt{3} \gamma_{m0}} + \frac{0.9 A_{tn} f_u}{\gamma_{m1}}$$

$$A_{vg} = [(e+P) t] \times 2$$

$$= [(33+60) 8] \times 2$$

$$\Rightarrow \boxed{A_{vg} = 1488 \text{ mm}^2}$$

$$A_{vn} = \left[(e+P - d_h - \frac{d_h}{4}) t \right] \times 2$$

$$A_{vn} = \left[(33+60 - 22 - \frac{22}{4}) \times 8 \right] \times 2$$

$$\Rightarrow \boxed{A_{vn} = 1048 \text{ mm}^2}$$

$$A_{tn} = \left[P t - \frac{d_h}{4} + \frac{d_h}{4} \right] \times t$$

$$= \left[60 \times 8 - \frac{22}{4} + \frac{22}{4} \right] 8$$

$$\Rightarrow \boxed{A_{tn} = 392 \text{ mm}^2}$$

$$T_{db1} = \frac{1488 \times 250}{\sqrt{3} \times 1.1} + \frac{0.9 \times 392 \times 410}{1.25}$$

$$\Rightarrow T_{db1} = 310967.76 \text{ N}$$

$$\Rightarrow T_{db1} = 310.97 \text{ kN} \Rightarrow$$

$$T_{db2} = \frac{0.9 A_v n f_0}{\sqrt{3} \gamma_{m2}} + \frac{A_t g f_y}{\gamma_{m0}}$$

$$\begin{aligned} A_t g &= P \times t \\ &= 60 \times 8 \\ &= 480 \text{ mm}^2 \end{aligned}$$

$$T_{db2} = \frac{0.9 \times 1048 \times 410}{\sqrt{3} \times 1.25} + \frac{480 \times 250}{1.1}$$

$$\Rightarrow T_{db2} = 287705.53 \text{ N}$$

$$\Rightarrow \boxed{T_{db2} = 287.7 \text{ kN}}$$

T_{db} = smaller of T_{db1} & T_{db2}

$$T_{db1} = 310.97 \text{ kN}$$

$$T_{db2} = 287.7 \text{ kN}$$

$$\boxed{T_{db} = T_{db2} = 287.7 \text{ kN}}$$

Strength of beam shear = 287.7 kN > 225 kN

So, it is safe.

COMPRESSION MEMBERS

Two equal & opposite compressive forces applied at any structural member's end then that member is called as compression member

Ex - strut, principal rafter / strut, top chord of truss, bracing member, boom in crane, and column/post (standing)

General failure of compression member

→ very short column or short strut is subjected axial compressive load. May generally fail by yielding or crushing of material.

→ very long column fail by elastic buckling in the Euler mode.

→ intermediate column or strut generally fail by elastic buckling compressive

Design strength of compression members:

$$\text{Design compressive strength} = P_d = f_{cd} \times A_e \quad (P < P_d)$$

Where, P = External compressive load

$$f_{cd} = \chi \cdot \frac{f_y}{\gamma_{m0}} \leq \frac{f_y}{\gamma_{m0}}$$

100) → χ = stress reduction factor

$$\chi = \frac{1}{\phi + [\phi^2 - \lambda^2]^{0.5}}$$

ϕ = stress factor

λ = effective slenderness ratio

$$\phi = 0.5 [1 + \alpha(\lambda - 0.2) + \lambda^2]$$

$f_{cr} = \rightarrow \alpha =$ imperfection factor from table (pg. 35)

$\lambda =$ effective slenderness ratio = $\sqrt{\frac{f_y}{f_{cc}}}$

$$f_{cc} = \frac{\pi^2 E}{\left(\frac{KL}{r}\right)^2} = \text{Euler buckling stress}$$

Buckling classification (pg. 44)

Q. What will be the buckling class of IHB 400 @ 907 N/mm² about z-z & y-y axis?

Ans. From steel table IHB 400 (taking overall depth 400 mm, weight/length or mm) $t_f = 12.7$ mm

$$h = 400 \text{ mm}$$

$$b_f = 250 \text{ mm}$$

$$\frac{h}{b_f} = \frac{400}{250} = 1.6 > 1.2$$

for z-z axis buckling class - a

for y-y axis buckling class - b

Limiting (or) maximum slenderness ratio (By WSM & LEM) $\lambda_{lim} (or) \lambda_{max}$

- (1) A member carrying compressive loads from dead & imposed load. $\rightarrow 180$
- (2) A member carrying compressive loads due to $\rightarrow 250$ only ~~weight~~ wind load & seismic load
- (3) For compressive flange or beam section or z-section, restrained against torsional buckling $\rightarrow 300$

$$[\text{long} = \text{member}(\lambda)]$$

calculate the design compressive load for an IHB 250 @ 536.6 N/m, 4m height. The column is restrained in direction only at both the ends. It is to be used as an unbraced column in a single storey building.

given data
height of column = 4m = L
IHB 250 @ 536.6 N/m

effective length = l = 0.65 L
= 0.65 x 4
= 2.6 m

IHB 250 @ 536.6 N/m

- ⇒ Depth of section (h) = 250 mm
- width of flange = b_f = 250 mm
- thickness of flange = t_f = 9.7 mm
- thickness of web = t_w = 8.8 mm

$\frac{h}{b_f} = \frac{250}{250} = 1 < 1.2$

t_f = 9.7 mm < 40 mm

$\frac{h}{b_f} = \frac{250}{250} = 1 < 1.2$

t_f = 9.7 mm < 100 mm

about z-z axis ⇒ buckling class = b

about y-y axis ⇒ buckling class = c

A_e = 69.71 cm² = 0.006971 m²

about z-z axis (b)

Design compressive strength = P_d = f_{cd} × A_e

f_{cd} = $\chi \times \frac{f_y}{\gamma_{m0}}$

$$\chi = \frac{1}{[\phi + (\phi^2 - \lambda)^{0.5}]}$$

$$\phi = 0.5 [1 + \alpha (\lambda - 0.2) + \lambda^2]$$

$\alpha = 0.34$ (buckling class 'b')
(Assume $f_e = 411$ steel $\Rightarrow f_{cc} = 410 \text{ MPa}$)

$$\lambda = \sqrt{\frac{f_y}{f_{cc}}}$$

$$f_{cc} = \frac{\pi^2 E}{\left(\frac{KL}{r_{zz}}\right)^2} = \frac{\pi^2 \times 2 \times 10^5}{\frac{0.65 \times 4}{107 \text{ mm}}^2}$$

$E = 2 \times 10^5$, $\pi_{zz} = 10.7 \text{ cm}$
 $f_y = 250 \text{ N/mm}^2$
 $r_{yy} = 53.7 \text{ mm}$
 $r_{zz} = 107 \text{ mm}$

$$= \frac{\pi^2 \times 2 \times 10^5}{\left(\frac{0.65 \times 4 \times 1000}{107}\right)^2} = 3343$$

$$\lambda = \sqrt{\frac{f_y}{f_{cc}}} = \sqrt{\frac{250}{3343}} = 0.27$$

$$\phi = 0.5 [1 + \alpha (\lambda - 0.2) + \lambda^2]$$

$$= 0.5 [1 + 0.34 (0.27 - 0.2) + 0.27^2]$$

$$= 0.548$$

$$\approx 0.55$$

$$\chi = \frac{1}{\phi + (\phi^2 - \lambda)^{0.5}} = \frac{1}{0.55 + (0.55^2 - 0.27)^{0.5}} = 0.97$$

$$f_{cd} = \chi \times \frac{f_y}{\gamma_{mo}} = 0.97 \times \frac{250}{1.1} = 220.45 \text{ N/mm}^2$$

$$\gamma_{mo} = 1.1$$

$$f_{cd} = 220.45 \text{ N/mm}^2$$

$$P_d = f_{cd} \times A_e$$

$$= 220.45 \times 6971$$

$$= 1536756.95 \text{ N} = 1536 \text{ kN}$$

$$A_e = 69.71 \text{ cm}^2$$

$$= 6971 \text{ mm}^2$$

About YY axis \Rightarrow buckling class = C $\alpha = 0.49$

$$\lambda = \frac{f_y}{f_{cc}}, f_{cc} = \frac{\pi^2 E}{\left(\frac{KL}{r_{yy}}\right)^2} = \frac{\pi^2 \times 2 \times 10^5}{\left(\frac{2.6 \times 10^3}{53.7}\right)^2} = 842$$

$$\lambda = \sqrt{\frac{f_y}{f_{cc}}} = \sqrt{\frac{250}{842}} = 0.54$$

$$\phi = 0.5 [1 + \alpha (\lambda - 0.2) + \lambda^2] = 0.5 [1 + 0.49 (0.54 - 0.2) + 0.54^2] = 0.73$$

$$f_{cd} = \frac{f_y / \gamma_{mo}}{\phi + (\phi^2 - \lambda)^{0.5}} = \frac{250 / 1.1}{0.73 + [0.73^2 - 0.54^2]^{0.5}} = 186.1$$

$$\text{Design compressive load} = P_d = f_{cd} \times A_e$$

$$= 186.1 \times 69.71 = 12973.5 \text{ kN} = 12.97 \text{ N/mm}^2$$

Design a column section to carry a working axial load of 400 kN. The column is 4m long & effectively held in position & restrain against rotation at both ends. Consider $f_y = 250 \text{ MPa}$

Given data

working axial load = 400 kN
 factored axial load = $400 \times 1.5 = 600 \text{ kN}$
 length of the column = 4m = $4 \times 1000 = 4000 \text{ mm}$
 $f_y = 250 \text{ N/mm}^2$

fixed @ both end $\Rightarrow K = 0.65$

let us assume the column section is beam.

Assume slenderness ratio = 90 = λ

\Rightarrow From table \rightarrow table 9(a) $\Rightarrow f_{cd} = 149 \text{ MPa}$ about z-z axis

From table \rightarrow table 9(b) $\Rightarrow f_{cd} = 134 \text{ MPa}$ about y-y axis

\therefore $f_{cd} = 134 \text{ MPa}$ $\left(\because \text{Because about y-y axis buckling will occur first} \right)$

$f_y = 250 \text{ MPa}$
 $\lambda = 90$
 buckling class = a about z-z axis
 buckling class = a about y-y axis

\Rightarrow Required Area =

$$= \frac{\text{Factored Axial Load}}{\text{Design compressive stress}} = \frac{600 \times 10^3 \text{ N}}{134 \text{ N/mm}^2} = 4477.61 \text{ mm}^2$$

let us take the section ISHB 200 @ 365.9 N/m

Area (A) = 47.54 cm^2 , $r_{zz} = 8.71 \text{ cm}$, $r_{yy} = 4.51 \text{ cm}$

$h = 200 \text{ mm}$, $b_f = 200 \text{ mm}$, $t_f = 9 \text{ mm}$

As $\frac{h}{b_f} = \frac{200}{200} = 1 \neq 1.2 \Rightarrow$ It will not satisfy our assumption for buckling class

\therefore again assume the section ISMB 250 @ 365.9 N/m

$A = 47.55 \text{ cm}^2$, $h = 250 \text{ mm}$, $r_{zz} = 10.39 \text{ cm}$,

$r_{yy} = 2.65 \text{ cm} = 26.5 \text{ mm}$, $b_f = 125 \text{ mm}$, $t_f = 12.5 \text{ mm}$

$\frac{h}{b_f} = \frac{250}{125} = 2 > 1.2$, $t_f = 12.5 \leq 40 \text{ mm}$

Effective length of column = $KL = 0.65 \times 4000 = 2600$

Effective slenderness ratio = $\frac{KL}{r_{yy}} = \frac{0.65 \times 4000}{26.5} = 98.11$

buckling class (b) and f_y 250, $\frac{KL}{r_{yy}} = 98.11$

$\frac{KL}{r_{yy}}$	f_{cd}
90	134
78.11	
100	118

$$f_{cd} = 134 - \frac{134 - 118}{100 - 90} \times (98.11 - 90)$$

$$= 121.02 \text{ N/mm}^2$$

\therefore the design compressive load $= P_d = f_{cd} \times A_e$

$$= 121.02 \times 4755$$

$$= 575450 \text{ LN}$$

$$\Rightarrow P_d = 575 \text{ KN} < 600 \text{ KN}$$

So not safe
So not safe

\therefore The section should be taken ISMB 300 @ 433.6 N/m

Then it will satisfy the load 600 KN.

effective length of column $= KL = 0.65 \times 4000 = 2600$

$A = 56.26 \text{ mm}^2$, $h = 300 \text{ mm}$, $b_f = 140 \text{ mm}$, $t_f = 12.4 \text{ mm}$

$r_{xx} = 12.37 \text{ cm}$, $r_{yy} = 2.84 \text{ cm} = 28.4 \text{ mm}$

effective slenderness ratio $= \frac{KL}{r_{yy}} = \frac{0.65 \times 4000}{28.4} = 91.55$

buckling class (b) of f_y 250, $\frac{KL}{r_{yy}} = 91.55$

$\frac{KL}{r_{yy}}$	f_{cd}
90	134
91.55	
100	118

$$f_{cd} = 134 - \frac{134 - 118}{100 - 90} \times (91.55 - 90)$$

$$= 131.51 \text{ KN/mm}^2$$

\therefore the design compressive load

$$P_d = f_{cd} \times A_e$$

$$= 131.51 \times 5626 = 739 \text{ KN}$$

$$= 739 \text{ KN} > 600 \text{ KN}$$

D.13.02.2020
1st half

CA-05

STEEL COLUMN BASES & FOUNDATIONS

Design compressive stress in a concrete footing is much smaller than it is in a steel column, so it is necessary to distribute the load from steel column and evenly to the footing below.

Types of Column Bases

- 1) Slab base
- 2) Gusset base
- 3) Grillage foundation

(1) Slab Base

Suitability

- It is most suitable for the column subjected to axial load.
- It is suitable for column subjected to light or less intensity of loads.
- A slab base is assumed to be hinged (pinned) base which can not resist lateral load.

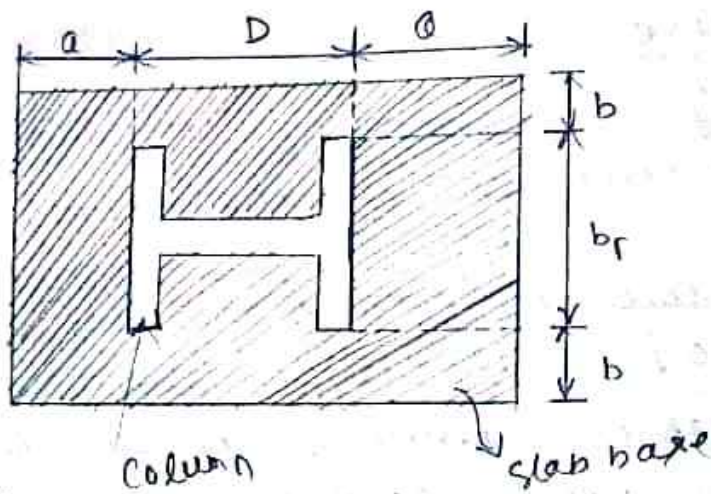
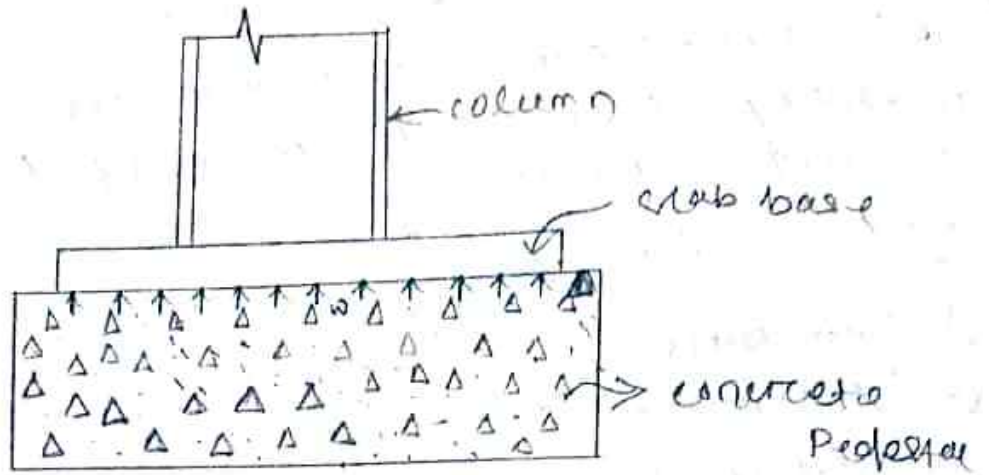
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NOTE

Design bearing strength of concrete = $0.45 f_{ck}$

~~Formula for slab base~~

9mp
Design procedure for slab base



D = overall ^{depth} width of column section

a = larger projection of slab base plate beyond column in mm

b = smaller projection of slab base plate beyond column in mm

b_f = width of the flange.

(E) Area of base plate required = $A_{base} = \frac{P}{0.45 f_{ck}} = \frac{\text{load}}{\text{bearing stress}}$

→ If a square base plate is provided, then the side of slab base = $\sqrt{A_{base}}$

→ If a rectangular ^{slab} base plate is provided, then

Area $A = L \times B = (D + 2a)(b_f + 2b)$

To have optimum thickness of slab base, the condition should be $a = b$, so area $- A = (D + 2a)(b_f + 2a)$
 $\Rightarrow a = ?$

(ii) Upward pressure from concrete pedestal below the slab base = $\frac{\text{factored}}{\text{area load of the column}} (P)$

Provided area of the slab base (A_{provided})

$$w = \frac{P}{A_{\text{provided}}} \leq 0.45 f_{ck}$$

(iii) Minimum thickness of rectangular slab base =

$$t_s = \sqrt{\frac{2.5 w (a^2 - 0.36 a^2) \gamma_{m0}}{f_y}}$$

Q.18 Design a slab base for a column ISHB 350 @ 710.2 $\frac{N}{mm^2}$ subjected to a factored load of 1500 kN. The base plate is raised on a concrete pedestal of M25 grade of concrete. Provide welded connection between column & base plate @

Sol

ISHB 350 @ 710.2 $\frac{N}{mm^2}$
 Overall depth
 $- D = 350 \text{ mm}$

Width of flange (b_f) = 250 mm

Factored load = $P = 1500 \text{ kN} = 1500 \times 10^3 \text{ N}$

M25 concrete $\Rightarrow f_{ck} = 25 \text{ MPa}$

Assume $f_u = 410 \text{ MPa}$, $f_y = 250 \text{ MPa}$

Area of base required = $A_{\text{base}} = \frac{P}{0.45 f_{ck}}$
 $= \frac{1500 \times 10^3}{0.45 \times 25}$

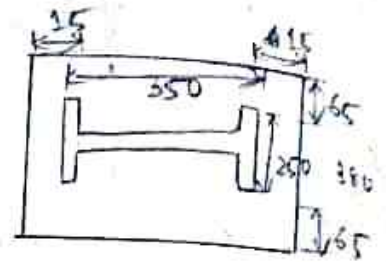
$\Rightarrow A_{\text{base}} = 133333.33 \text{ mm}^2$

Let us provide a square slab base base

$$\begin{aligned} \Rightarrow \text{side of base plate} &= \sqrt{A_{\text{base}}} \\ &= \sqrt{133333.33} \\ &= 365.15 \text{ mm} \end{aligned}$$

Now provide a square slab base of size = 380 mm

$$\begin{aligned} \Rightarrow \text{provided Area} &= (380)^2 \\ (A_{\text{provided}}) &= 144400 \text{ mm}^2 \end{aligned}$$



larger projection of slab base = $a = \frac{380 - 250}{2} = 65 \text{ mm}$

smaller projection of slab base = $b = \frac{380 - 350}{2} = 15 \text{ mm}$

Minimum thickness of rectangular upward pressure from concrete pedestal below slab base = $w = \frac{P}{A_{\text{provided}}}$ (provided Area of the slab base)

$$= \frac{1500 \times 10^3}{380^2} \leq 0.45 f_{cu}$$

$$= 10.38 \text{ N/mm}^2 \leq 0.45 \times 25$$

$$= 10.38 \text{ N/mm}^2 \leq 11.25 \text{ (safe)}$$

Minimum thickness of rectangular slab area

$$t_s = \sqrt{\frac{2.5w(a^2 - 0.36^2)}{\gamma_{mo}}}$$

$$= \sqrt{\frac{2.5 \times 10.38 (65^2 - 0.9 \times 15^2)}{1.1}}$$

$$\Rightarrow t_s = 21.8 \text{ mm} \therefore \text{size of the slab base } (380)^2 (21.8) \text{ mm} = 3133480 \text{ mm}^2$$

Actual effective length of weld (l_w)

~~$=(250+250) \times 2 \times 11.6$~~

[thickness of flange (t_f) = 11.6]

~~$l_w = [(250+250 + (350 - 2 \times 11.6))] \times 2$~~

$l_w = 1653.6 \text{ mm}$

effective throat thickness (t_e)

$t_e = k_s$

$s_{max} = \frac{3}{4} t_{min}$

$11.6 = \frac{3}{4} \times 11.6$

$s_{min} = 8.7$

$\therefore s_{min} = 5$

$\therefore \text{size of weld} = 8 \text{ mm}$

$t_e = k_s$

$= 0.7 \times 8$

$= 5.6 \text{ mm}$

\Rightarrow Strength of weld = P_{dw}

$P_{dw} = (L_w t_e) \left(\frac{f_u}{\sqrt{3} \gamma_{mw}} \right)$

$\Rightarrow P_{dw} = P = (L_w t_e) \frac{f_u}{\sqrt{3} \gamma_{mw}} \quad [\because P = \text{factored load}]$

$\Rightarrow 1500 \times 10^3 = (l_w \times 5.6) \cdot \frac{410}{\sqrt{3} \times 1.25}$

$\Rightarrow 1500 \times 10^3 = (l_w \times 5.6) \times 189.37$

$\Rightarrow \frac{1500 \times 10^3}{189.37} = (l_w \times 5.6)$

$$\Rightarrow 7921 = l_w \times 5.6$$

$$\Rightarrow l_w = \frac{7921}{5.6}$$

$$\Rightarrow l_w = 1414.46 \text{ mm}$$

\Rightarrow Required effective length of weld = 1414. mm

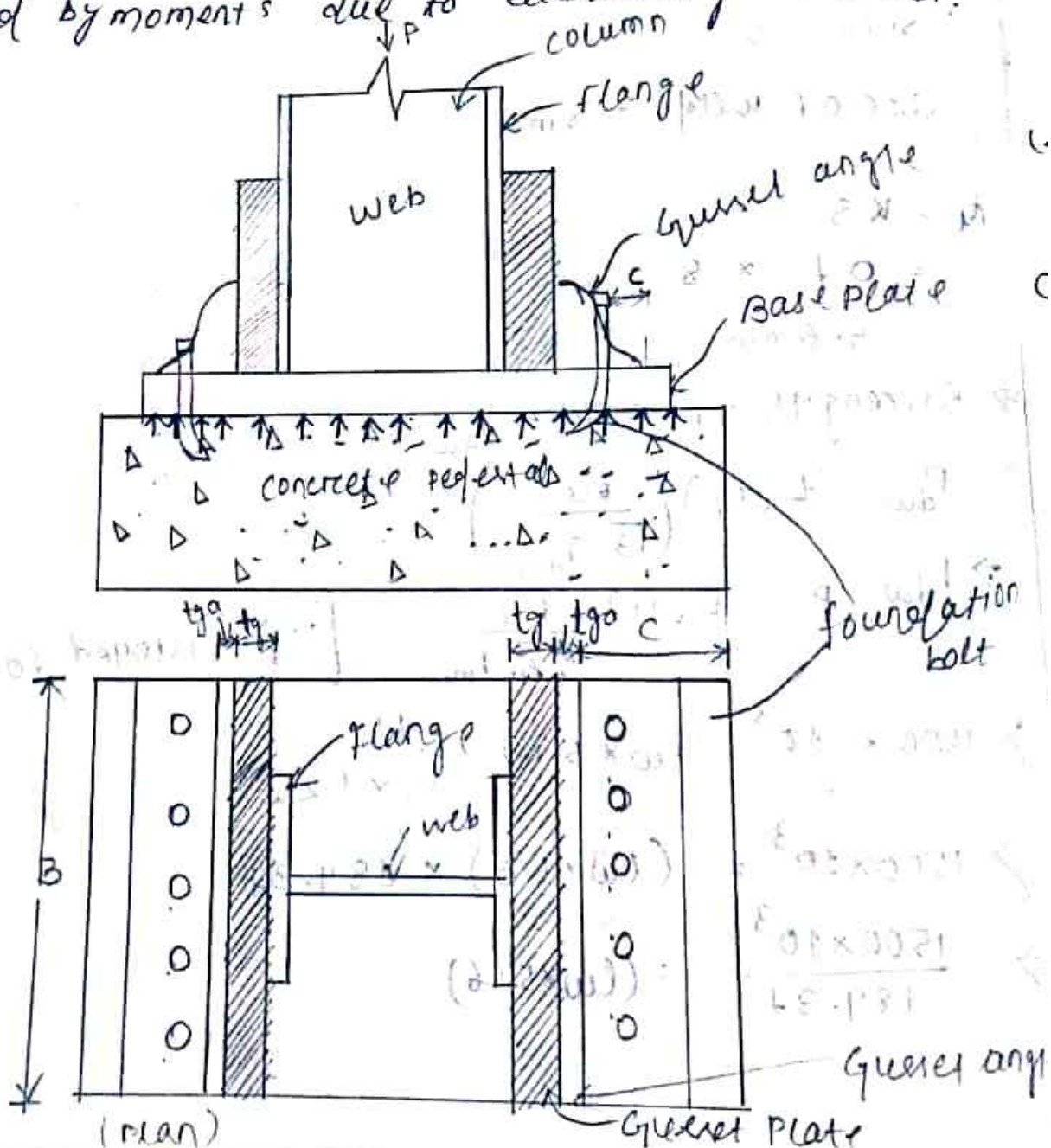
$$< (l_w)_{\text{actual}} = 1653 \text{ mm}$$

\therefore Which is safe design.

D. 17.02.2020

(2) Gusseted Base

Gusseted base is normally used when steel column is subjected to heavy axial compressive loads as well as when steel column is subjected to axial loads & accompanied by moments due to eccentricity of loads.



$B \& L$ = Width or length of the base plate respectively
 C = cantilever projection of the base plate from root of the gusset angle.

t_g = Thickness of gusset plate

t_{ga} = Thickness of gusset angle

D = Depth of steel column

$b_f \& t_f$ = Width & thickness of column flange

(i) Area of base plate required = $A_{required}$

$$A_{required} = \frac{\text{Design axial compressive load (P)}}{\text{Design bearing strength of concrete}}$$

$$A_{base, required} = \frac{P}{0.45 f_{ck}}$$

$$\Rightarrow \left[A_{provided} = \text{more value than } A_{required} \right]^*$$

(ii) Length of the base plate required

$$L = D t_2 (t_g + t_{ga} + e.)$$

(iii) Upward pressure from concrete per unit area below the base plate =

$$w = \frac{\text{Design axial compressive load (P)}}{\text{provided Area of the base plate (A}_{provided}\text{)}}$$

(iv) Thickness of gusset plate = $t_g = c \sqrt{\frac{2.75 w}{f_y}}$

(v) Thickness of base plate = $t_b = t_g$ (in case of welded connection)
 $t_b = t_g - t_{ga}$ (in case of bolted connection)

D. 18. 02. 2020

Ch-06

DESIGN OF STEEL BARS

- A structural member subjected to transverse load (load \perp to its longitudinal axis) is called beam.
- when provided in buildings to support roofs, they are called joist.
- A large beam supporting a no. of joists is called girder.
- Beam which carry the roof loads in trusses are called purlins.
- Beam which support the loads from masonry over the openings are called lintels.

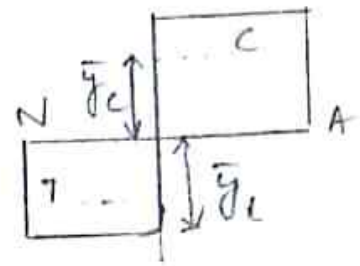
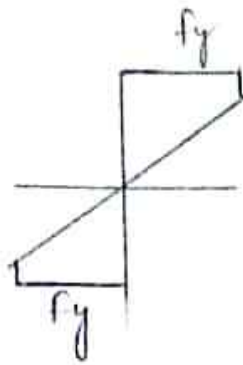
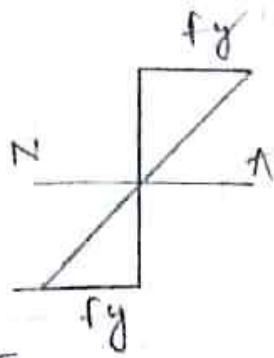
Beam

Plastic moment capacity of beam section (M_p):-

$$M_p = f_y \cdot Z_p$$

where, Z_p = plastic section mod.

f_y = yield stress material



$$\frac{M}{I} = \frac{f}{y} = \frac{E}{R}$$

$$M = f \frac{I}{y} = f_y \cdot z$$

$$M_p = f_y \cdot z_p$$

$$z_p = \frac{A}{2} (\bar{y}_c + \bar{y}_t)$$

$$= A_c \bar{y}_c + A_t \bar{y}_t$$

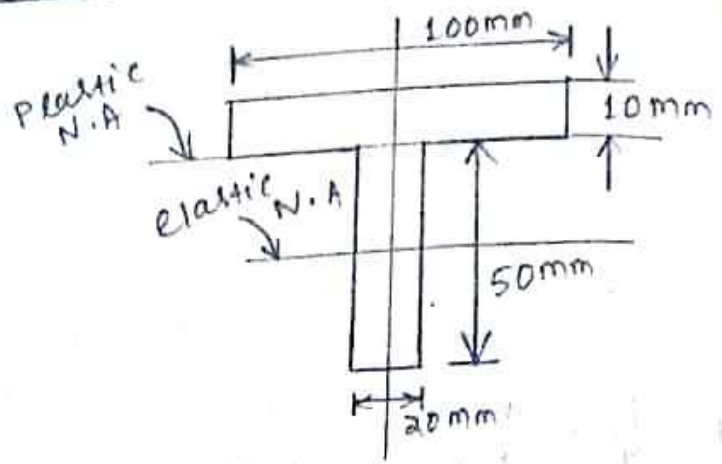
A_c & A_t are area under compression and tension respectively.

\bar{y}_c & \bar{y}_t are centroidal distance of compression & tension area from the plastic neutral axis respectively.

Area under compression = Area under tension.

NOTE

- Plastic neutral axis divides the total area into two equal halves.
- Elastic neutral axis always pass through the C.G.
- For symmetrical section (about x-axis) the elastic N-A & plastic N-A will coincide.
- For unsymmetrical section (about x-axis) the elastic N-A and plastic N-A will not coincide.



$$\text{ELASTIC N.A.} = (\bar{y}) = \frac{A_1 y_1 + A_2 y_2}{A_1 + A_2}$$

FROM BOTTOM

$$= \frac{1000 \times (50 + \frac{10}{2}) + (50 \times 20) \times (\frac{50}{2})}{1000 + 1000}$$

$$= 40 \text{ mm}$$

PLASTIC N.A. FROM BOTTOM = 50 mm FROM BOTTOM

$$A = (100 \times 10) + (50 \times 20) = 2000$$

$$\frac{A}{2} = \frac{2000}{2} = 1000$$

Ex

$$M_p = f_y Z_p$$

$$= f_y \left[\frac{A}{2} (\bar{y}_c + \bar{y}_H) \right]$$

$$= f_y \left[\frac{bh}{2} \left(\frac{h}{2} + \frac{h}{2} \right) \right]$$

$$M_p = f_y \left[\frac{bh}{2} \times \frac{h}{2} \right]$$

$$\Rightarrow \boxed{M_p = f_y \frac{bh^2}{4}}$$

Problem Determine the plastic moment capacity of an asymmetrical I-section. Given size :-

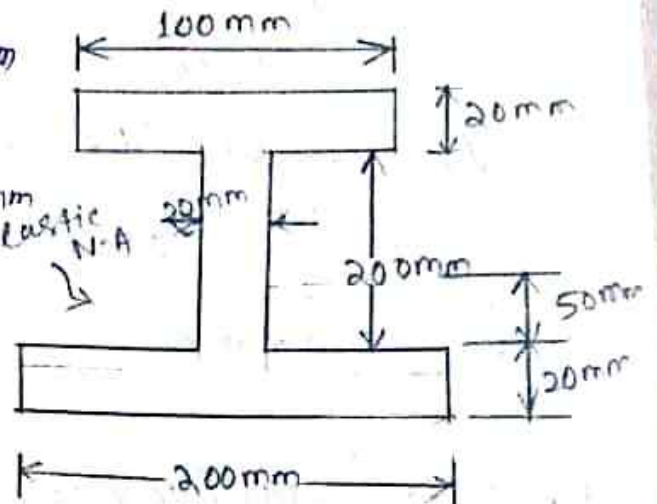
Top Flange = 100mm x 20mm
 bottom flange = 200mm x 20mm
 Web = 200mm x 20mm

Solution

Area of Top flange = 100mm x 20mm
 = 2000mm²

Area of bottom flange = 200mm x 20mm
 = 4000mm²

Area of web = 200mm x 20mm
 = 4000mm²



Total Area = 2000 + 4000 + 4000
 = 10000 mm²

Plastic N-A = $\frac{A}{2} = \frac{10,000}{2} = 5000 \text{ mm}^2$

$$\left. \begin{aligned} \text{Area} &= bh \\ \Rightarrow 1000 &= 20h \\ \Rightarrow h &= \frac{1000}{20} \\ \Rightarrow h &= 50 \text{ mm} \end{aligned} \right\}$$

$$\frac{A}{2} = A_c = A_t$$

$$M_p = f_y Z_p$$

$$= f_y \left[\frac{A}{2} (\bar{y}_c + \bar{y}_t) \right]$$

$$= f_y (A_c \bar{y}_c + A_t \bar{y}_t)$$

$$= f_y [5000 (\bar{y}_c + \bar{y}_t)]$$

\bar{y}_c = centroidal distance of compression area from plastic N-A

$$\bar{y}_c = \frac{A_1 y_1 + A_2 y_2}{A_1 + A_2}$$

$$\Rightarrow \bar{y}_c = \frac{(100 \times 20) (150 + 10) + (150 \times 20) (\frac{150}{2})}{(100 \times 20) + (150 \times 20)}$$

$$\Rightarrow \boxed{\bar{y}_c = 109 \text{ mm}}$$

\bar{y}_t = centroidal distance of tension area from PLASTIC N-A

$$\bar{y}_t = \frac{A_1 y_1 + A_2 y_2}{A_1 + A_2}$$

$$\Rightarrow \bar{y}_t = \frac{(200 \times 20)(50 \times 10) + (50 \times 20)(25)}{(200 \times 20) + (50 \times 20)}$$

$$\Rightarrow \boxed{\bar{y}_t = 53 \text{ mm}}$$

$$M_p = f_y [5000 (109 + 53)]$$

$$\Rightarrow \boxed{M_p = 81 \times 10^4 f_y \text{ N}\cdot\text{mm}}$$